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POSITRON PRODUCTION EFFICIENCY STUDY USING
HIGH REPETITION RATE LINAC AT IAC

by

Sadiq Setiniyaz
(Shadike Saitiniyazi)

A dissertation

submitted in partial fulfillment

of the requirements for the degree of

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Idaho State University

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2013

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Abstract

I propose to measure the positron production efficiency for a positron source that uses a quadrupole triplet system to collect positrons from a tungsten target that are produced when the target is impinged by electrons from the High Repetition Rate Linac (HRRL) at Idaho State University's (ISU) Idaho Accelerator Center (IAC). Positrons were observed in May of 2008 at the IAC without the use of a quadrupole triplet collection system. When a 10 MeV electron beam is used on the tungsten target, positrons escaping from the downstream side of the tungsten have a wide momentum spread of 0 to 2 MeV and a large divergence of π rad. A quad triplet collection system, after the tungsten target, is used to focus the positron beam and as a result increase our positron collection efficiency. I will install the collection system and associated beam line components and measure the positron production efficiency using the HRRL.

= Text = ==Introduction==

Chapter 1

Introduction

1.1 Positron Beam

Positrons have many potentials in many discipline of science, like chemistry, physics, material science, surface science, biology and nanoscience [1]. There are many different ways to generate positrons, and the main challenge is increasing the intensity (or current) of the positron beam. Positrons tend to annihilate where there is defects in the material. This can be applied for non-damaging detection of defects in the material [citation vakho thesis]. Being the anti-matter of electron, it can be used to as high density energy source via annihilation in long term perspective [citation]. Positrons can be transported to the cancer tumor and the radiation they emit in the annihilation can be used to kill the cancer cell [citation].

1.2 Motivation for Positron Beamline

The nucleon electromagnetic form factors are fundamental quantities that related to the charge and magnetization distribution in the nucleon. Conventionally, the nucleon form factors are measured using Rosenbluth Technique (RT) [2]. The form factor scaling ratio, $R = \mu_p G_{Ep}/G_{Mp}$, measured using this technique is around unity as shown in the figure below [3]. Since nighties, a technique using elastic electron-proton polarization transfer to measurement this ratio have been developed [3–5]. In this technique, form factor scaling ratio linearly decreases as the Q^2 increases, as shown in the Fig. 1.1.

The disagreement could arise from the fact the Rosenbluth Techqniue assumes that One

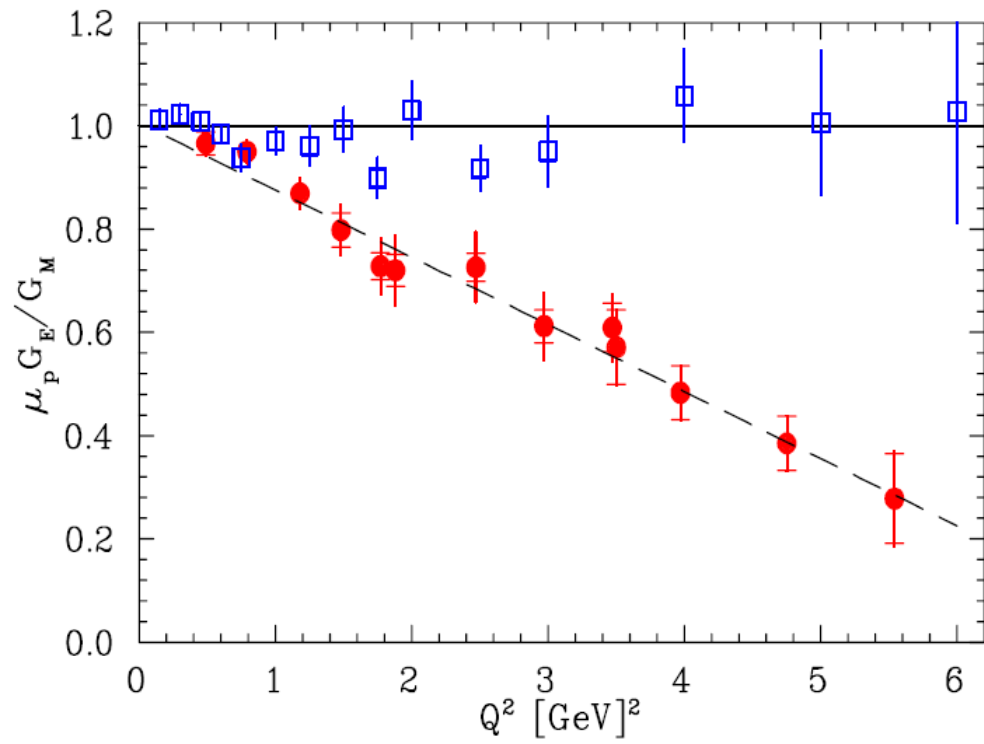


Figure 1.1: Form factor ratio, obtained by Rosenbluth Technique (hollow square) and results from Recoil Polarization Technique [4].

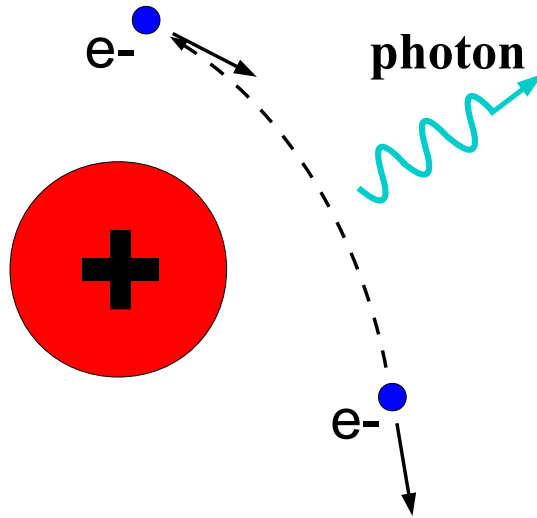


Figure 1.2: Photon generation from Bremsstrahlung processes.

Photon Exchange (OPE) during the scattering while the twophoton exchange (TPE), which depends weakly on Q^2 , could also become considerable with increasing Q^2 [4]. The contribution of TPE can be obtained by comparing the ratio of $e^+ p$ to $e^- p$ ratio. The interference of OPE and TPE can also be studied in the process $e^+e^- \rightarrow p\bar{p}$

1.3 Positron Beam Generation from Bremsstrahlung

When a moving charged particle interacts with the electric field of another charged particle, it can be deflected and lose energy in the form of photons, as shown in Fig. 1.2. This interaction is known as the Bremsstrahlung process. The probability of this interaction increases with the atomic number of the material traversed by the incident charged particle. Fig. 1.3 shows the photon energy distribution when a 12 MeV electron distribution from Fig. 1.4 interacts with a 1 mm thick Tungsten target. The number of photons in this example produced decreases as the energy of the produced photon increases. The Bremsstrahlung photons are also likely to interact with the material.

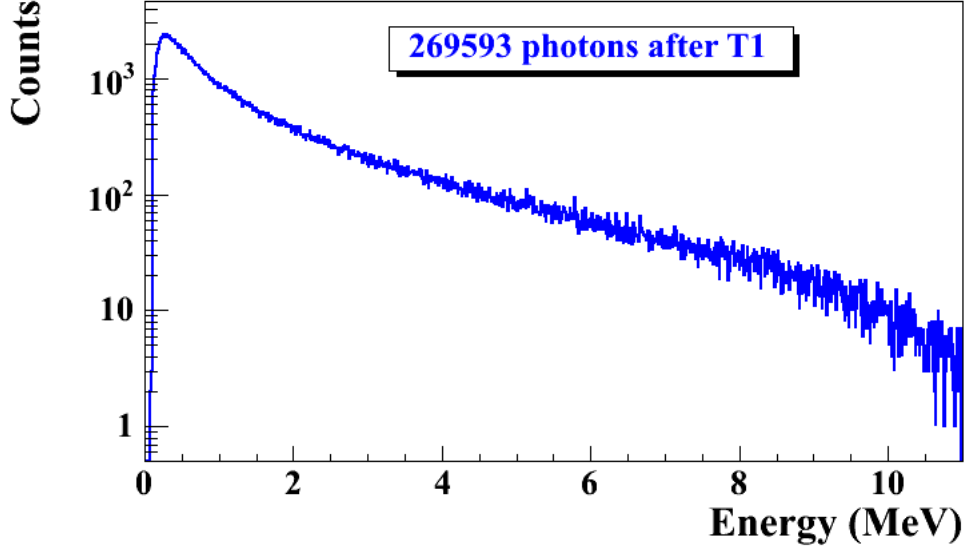


Figure 1.3: Simulated Bremsstrahlung photon energy right after a tungsten foil.

The cross section of Bremsstrahlung process is give by Eq. 1.1 [6]

$$d\sigma = 4Z^2 r_e^2 \alpha \frac{d\nu}{\nu} \left\{ \left(1 + \left(\frac{E}{E_0} \right)^2 \right) \left[\frac{\phi_1(\gamma)}{4} - \frac{1}{3} \ln Z - f(Z) \right] - \frac{2E}{3E_0} \left[\frac{\phi_2(\gamma)}{4} - \frac{1}{3} \ln Z - f(Z) \right] \right\} \quad (1.1)$$

where, E_0 is initial total energy of the electron, E is final total energy of the electron, $\nu = \frac{E_0 - E}{h}$ is energy of the emitted photon, and Z is atomic number. $\gamma = \frac{100m_e c^2 h\nu}{E_0 E Z^{1/3}}$ is charge screening parameter and $f(Z)$ is given by [7]

$$f(Z) = (Z\alpha)^2 \sum_1^{\infty} \frac{1}{n[n^2 + (Z\alpha)^2]} \quad (1.2)$$

where $\alpha = \frac{1}{137}$ is fine-structure constant, ϕ_1 and ϕ_2 are screening functions that depend on Z

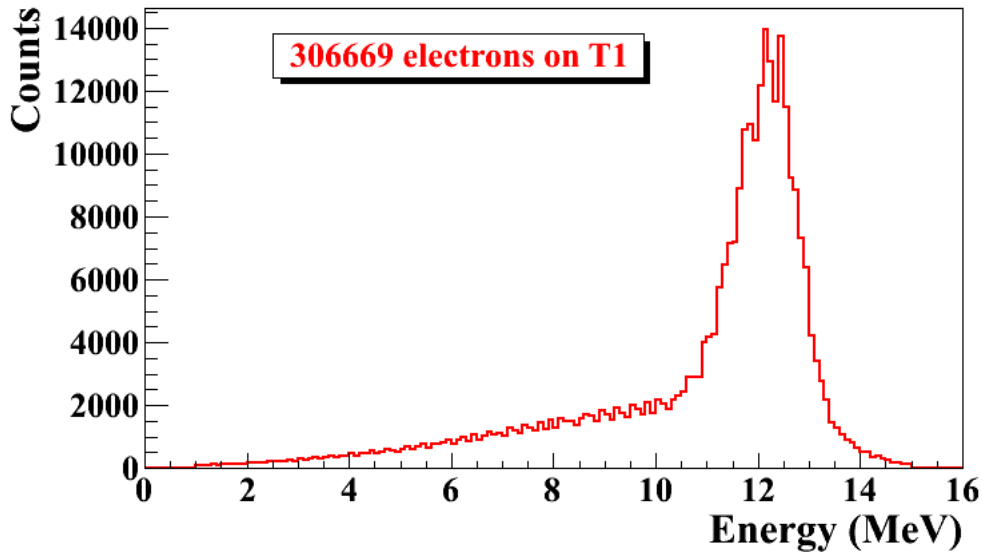


Figure 1.4: Simulated electron energy distribution right before a tungsten foil.

There are three competing processes that a photon can undergo when interacting with matter. At electron volt (eV) energies comparable to the electron atomic binding energy, the dominant photon interaction is via photoelectric effect. As the photon energy increases up to kilo-electron volt (keV) range, the Compton scattering process starts to be more dominant. Although the photon is totally absorbed during the photoelectric effect, photons merely lose energy when undergoing Compton scattering. As the photon energy reaches twice the rest mass energy of electron, 2×511 keV, pair production begins to happen. Pair production becomes dominant interaction process only for energies above 5 MeV [9]. In this process, a photon interacts with the electric field of the nucleus or the bound electrons and decays into an electron and positron pair.

Using natural unit $c \equiv 1$, the differential cross-section for pair production can be expressed as [7, 8],

$$\frac{d\sigma}{d\epsilon_1 d\theta_1 d\theta_2} = 8 \left(\frac{\pi a}{\sinh(\pi a)} \right)^2 \frac{a^2 e^2}{2\pi \hbar c} \left(\frac{\hbar}{m_e c} \right)^2 \frac{\epsilon_1 \epsilon_2}{k^3} \theta_1 \theta_2 \quad (1.3)$$

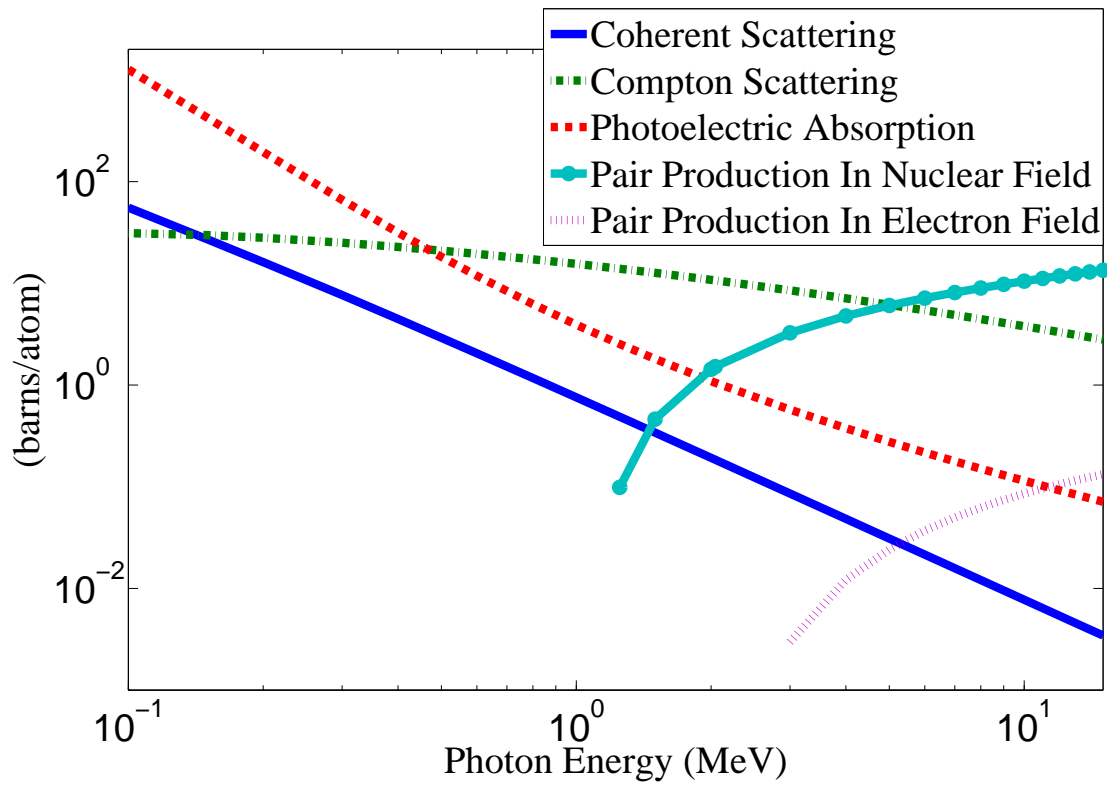


Figure 1.5: Cross section of processes that photons interacts with tungsten [10]

$$\begin{aligned}
& \times \left\{ \frac{V^2(x)}{q^4} [k^2(u^2 + v^2)\xi\eta - 2\epsilon_1\epsilon_2(u^2\xi^2 + v^2\eta^2) + 2(\epsilon_1^2 + \epsilon_2^2)uv\xi\eta\cos(\phi)] \right. \\
& \left. + a^2W^2(x)\xi^2\eta^2 [k^2(1 - (u^2 + v^2)\xi\eta - 2\epsilon_1\epsilon_2(u^2\xi^2 + v^2\eta^2) - 2(\epsilon_1^2 + \epsilon_2^2)uv\xi\eta\cos(\phi))] \right\} \quad (1.4)
\end{aligned}$$

where k is photon energy, θ_1 and θ_2 are the scattering angle of e^+ and e^- respectively, $\phi = \phi_1 - \phi_2$ is the angle between the e^+ and e^- pair, ϵ_1 and ϵ_2 are the energy of the positron and electron respectively. Other constants are $u = \epsilon_1\theta_1$, $v = \epsilon_2\theta_2$, $\xi = \frac{1}{1+u^2}$, $\eta = \frac{1}{1+v^2}$, $q^2 = u^2 + v^2 + 2uv\cos(\phi)$, $x = 1 - q^2\xi\eta$, $a = \frac{Ze^2}{\hbar c}$, and $V(x) = 1 + \frac{a^2}{(1!)^2} + \frac{a^2(1+a^2)x^2}{(2!)^2} + \frac{a^2(1+a^2)(2^2+a^2)x^4x^2}{(3!)^2} + \dots$, $W(x) = \frac{1}{a^2} \frac{dV(x)}{dx}$.

The positron and electron pairs are created back to back in the center of mass frame. In the lab frame, electrons and positrons are boosted forward, as demonstrated in the Fig. 1.6. The positron and electron carry away the energy from the photon that is in excess of 1.022 MeV. In the center of mass frame, the kinetic energy is equally shared. Photons with an energy above 1.022 MeV in the bremsstrahlung spectrum of Fig. 1.7 (a) have the potential to create electron and positron pairs. When the process of annihilation is included in the simulation, Fig. 1.7 (a) becomes Fig. 1.7 (b) showing a clear 511 keV peak on top of the bremsstrahlung spectrum. This 511 keV peak represents photon produced when the created positrons, from pair production, annihilates with an atomic electrons inside the tungsten target.

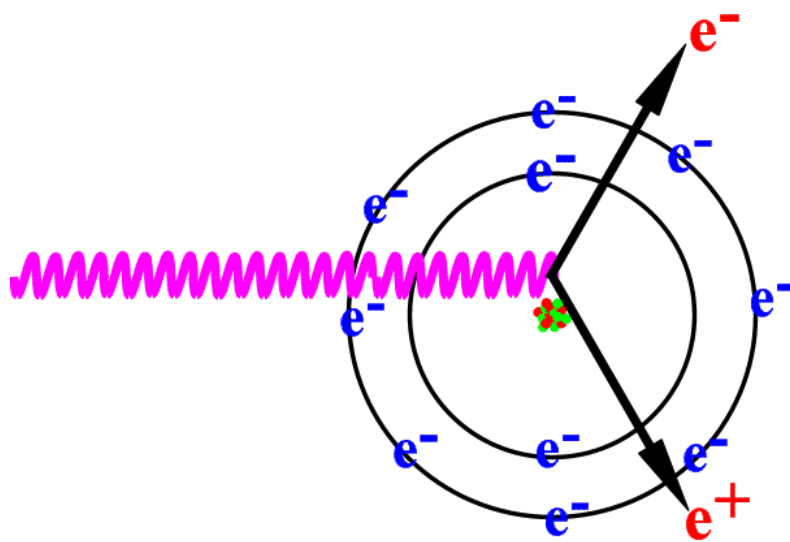
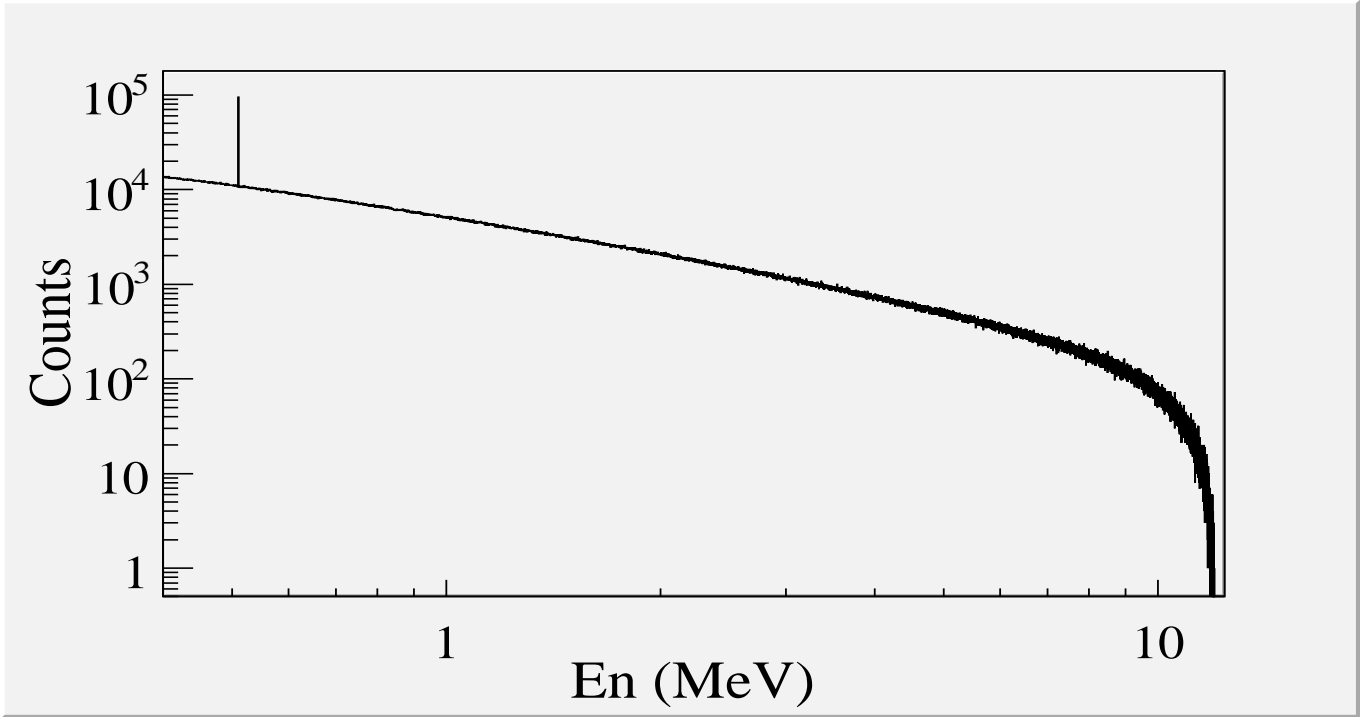
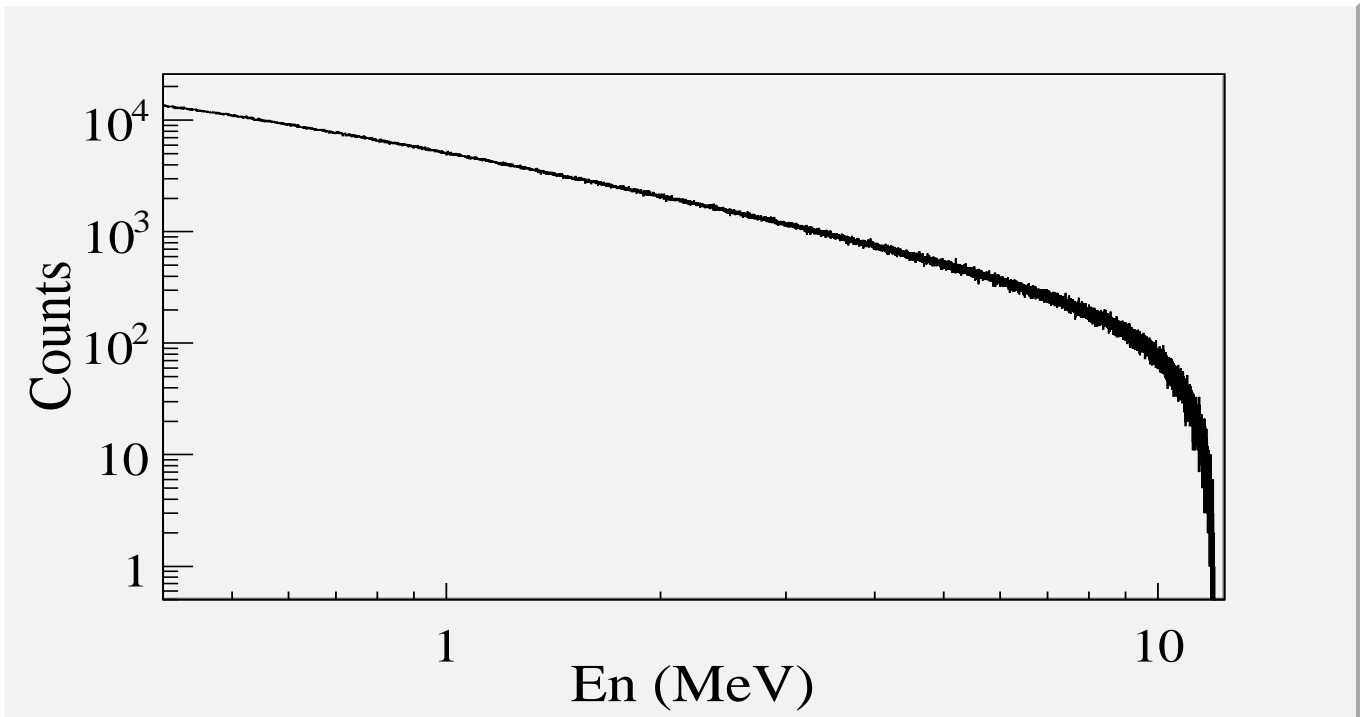


Figure 1.6: Pair production.



(a)



(b)

Figure 1.7: Bremsstrahlung photon spectrum (a) and Bremsstrahlung spectrum after turning on pair production process (b).

== Apparatus ==

Chapter 2

Apparatus

2.1 HRRL Beamline

The first step of this experiment is to deliver an electron beam with energy around 10 MeV and with sufficient current to the tungsten foil. A 16 MeV S-band High Repetition Rate Linac (HRRL) located at the Beam Lab of the Department of the Physics, Idaho State University is used to generate incident electron beam. The energy of the HRRL can be tunable between 3 to 16 MeV and its rep and its repetition rate is tunable between 1-300 Hz. Some basic parameters of the HRRL is given in the 2.1. To construct a beamline can run on both positron and electron mode, the cavity is relocated to its current position and quadrupole and dipole magnets to transport the beam. As shown in Fig. 2.1 and described in Tab. 2.2 more diagnostic tools like OTR/YAG screens, Faraday cups and toroids are installed to the new beamline for diagnostic purposes of electron beam. Energy slits are added to the beamline for the control of energy/momentum spread of the beam. A insertable tungsten foil target (T1) is placed between the 1st and 2nd triplets to produce positrons when the electron beam hits it.

Table 2.1: Emittance Measurement Results.

Parameter	Unit	Value
maximum energy	MeV	16
peak current	mA	100
repetition rate	Hz	300
absolute energy spread	MeV	2-4
macro pulse length	ns	>50

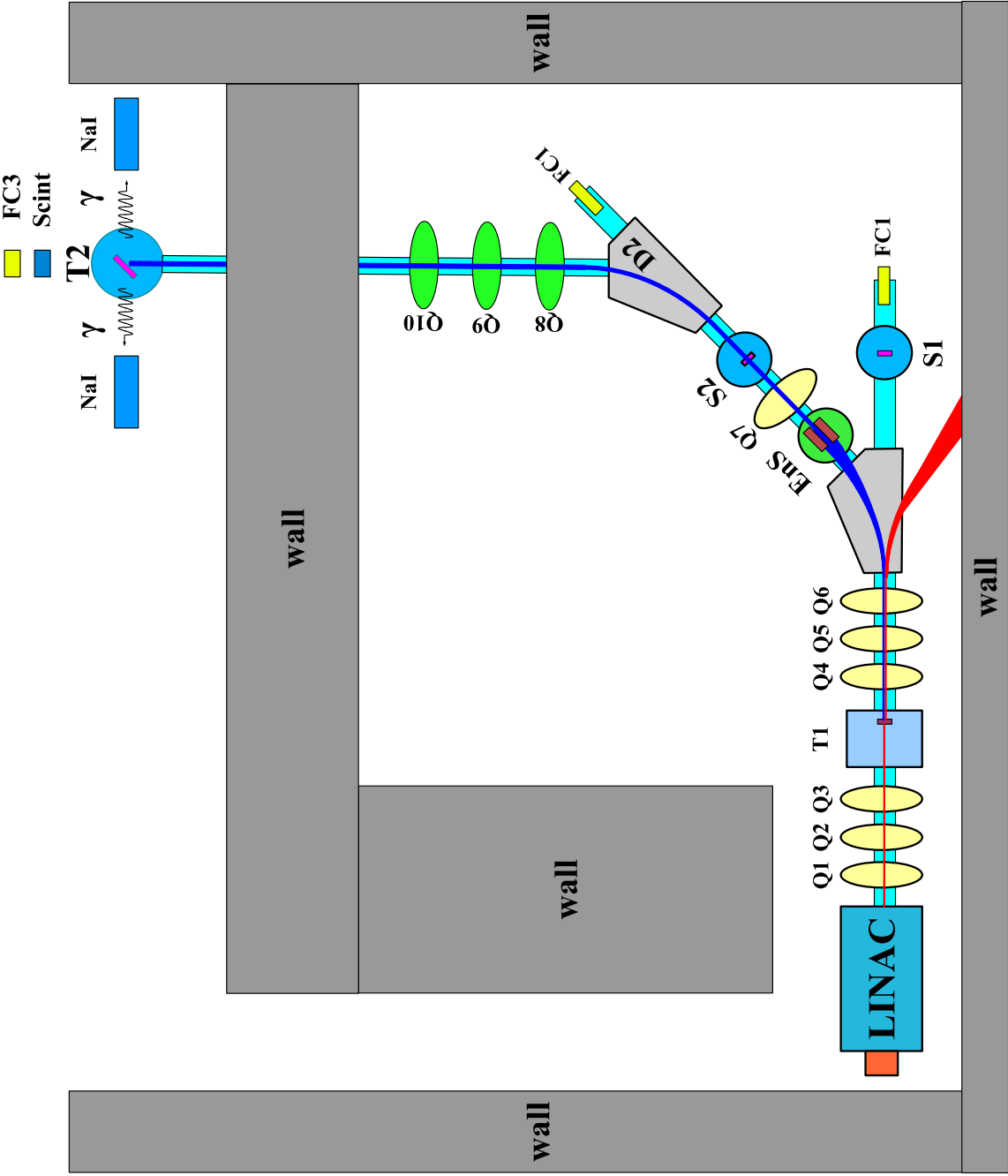


Figure 2.1: HRRL beamline layout and parts.

Table 2.2: HRRL Beamline Parts.

Label	Beamline Element
T1	positron production target
T2	positron annihilation target
Ens	energy slit
FC1, FC2	Faraday cups
Q1,..., Q10	quadrupoles
D1, D2	dipoles
NaI	NaI detectors
OTR	optical transition radiation screen
YAG	yttrium aluminium garnet screen

2.2 Electron Beam Characterization

2.2.1 Emittance Measurement

Emittance is an important parameter in accelerator physics. If emittance with Twiss parameters are given at the exit of the gun, we will be able to calculate beam size and divergence any point after the exit of the gun. Knowing the beam size and beam divergence on the positron target will greatly help us study the process of creating positron. Emittance with twiss parameters are also key parameters for any accelerator simulations. Also, energy and energy spread of the beam will be measured in the emittance measurement.

Emittance

In accelerator physics, Cartesian coordinate system was used to describe motion of the accelerated particles. Usually the z-axis of Cartesian coordinate system is set to be along the electron beam line as longitudinal beam direction. X-axis is set to be horizontal and perpendicular to the longitudinal direction, as one of the transverse beam direction. Y-axis is set to be vertical and perpendicular to the longitudinal direction, as another transverse beam direction. For the convenience of representation, we use z to represent our transverse coordinates, while discussing emittance. And we would like to express longitudinal beam

direction with s . Our transverse beam profile changes along the beam line, it makes z is function of s , $z(s)$. The angle of a accelerated charge regarding the designed orbit can be defined as $z' = \frac{dz}{ds}$.

If we plot z vs. z' , we will get an ellipse. The area of the ellipse is an invariant, which is called Courant-Snyder invariant [11]. The transverse emittance ϵ of the beam is defined to be the area of the ellipse, which contains 90% of the particles. Beam divergence and Twiss parameters related to the beam size and beam divergence by Eq. 2.1,

$$\sigma_x(s) = \sqrt{\epsilon_x(s)\beta_x(s)}, \quad \sigma_{x'}(s) = \sqrt{\epsilon_x(s)\gamma_x(s)}. \quad (2.1)$$

Emittance Measurement

The transition radiation first theoretically predicted by Ginzburg and Frank [12] in 1946, that when a particle with charge passes the boundary of two medium emits radiation. The particle carries certain field when it passes through certain medium with certain motion [13]. When it passes into the second medium, it has to reorganize its field characteristics at the boundary, and emit pieces of the field in the form electromagnetic radiation. The fields are emitted in the forward and backward directions [14]. The backward radiated photons

An Optical Transition Radiation (OTR) based viewer was installed to allow measurements at the high electron currents available using the HRRL. The visible light from the OTR based viewer is produced when a relativistic electron beam crosses the boundary of two mediums with different dielectric constants. Visible radiation is emitted at an angle of 90° with respect to the incident beam direction when the electron beam intersects the OTR target at a 45° angle. These backward-emitted photons are observed using a digital camera and can be used to measure the shape and intensity of the electron beam based on the OTR distribution. The emittance measurement can be performed in a several ways [15, 16]. The Quadrupole scanning method [18] was used to measure the emittance, Twiss parameters, and beam energy.

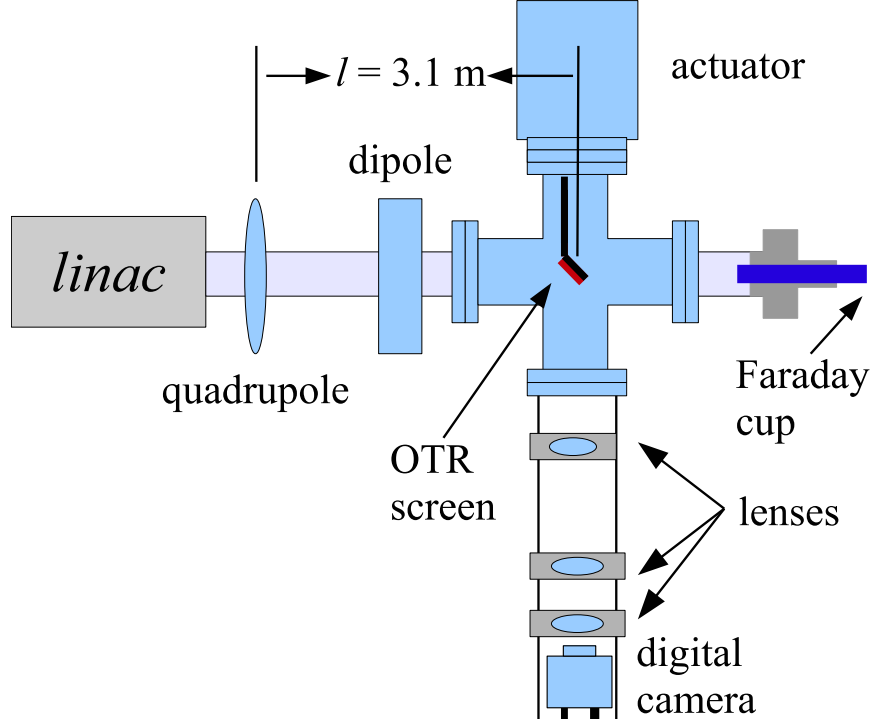


Figure 2.2: Apparatus used to measure the beam emittance.

Quadrupole Scanning Method

Fig. 2.2 illustrates the apparatus used to measure the emittance using the quadrupole scanning method. A quadrupole is positioned at the exit of the linac to focus or de-focus the beam as observed on a downstream view screen. The 3.1 m distance between the quadrupole and the screen was chosen in order to minimize chromatic effects and to satisfy the thin lens approximation. Assuming the thin lens approximation, $\sqrt{k_1 L} \ll 1$, is satisfied, the transfer matrix of a quadrupole magnet may be expressed as

$$\mathbf{Q} = \begin{pmatrix} 1 & 0 \\ -k_1 L & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ -\frac{1}{f} & 1 \end{pmatrix}, \quad (2.2)$$

where k_1 is the quadrupole strength, L is the length of quadrupole, and f is the focal length. A matrix representing the drift space between the quadrupole and screen is given by

$$\mathbf{S} = \begin{pmatrix} 1 & l \\ 0 & 1 \end{pmatrix}, \quad (2.3)$$

where l is the distance between the scanning quadrupole and the screen. The transfer matrix of the scanning region is given by the matrix product $\mathbf{S}\mathbf{Q}$. In the horizontal plane, the beam matrix at the screen (σ_s) is related to the beam matrix of the quadrupole (σ_q) using the similarity transformation

$$\sigma_s = \mathbf{M}\sigma_q\mathbf{M}^T. \quad (2.4)$$

where the σ_s and σ_q are defined as [17]

$$\sigma_{s,x} = \begin{pmatrix} \sigma_{s,x}^2 & \sigma_{s,xx'} \\ \sigma_{s,xx'} & \sigma_{s,x'}^2 \end{pmatrix}, \quad \sigma_{q,x} = \begin{pmatrix} \sigma_{q,x}^2 & \sigma_{q,xx'} \\ \sigma_{q,xx'} & \sigma_{q,x'}^2 \end{pmatrix}. \quad (2.5)$$

By defining the new parameters [18]

$$A \equiv l^2\sigma_{q,x}^2, \quad B \equiv \frac{1}{l} + \frac{\sigma_{q,xx'}}{\sigma_{q,x}^2}, \quad C \equiv l^2\frac{\epsilon_x^2}{\sigma_{q,x}^2}, \quad (2.6)$$

the matrix element $\sigma_{s,x}^2$, the square of the rms beam size at the screen, may be expressed as a parabolic function of the product of k_1 and L

$$\sigma_{s,x}^2 = A(k_1L)^2 - 2AB(k_1L) + (C + AB^2). \quad (2.7)$$

The emittance measurement was performed by changing the quadrupole current, which changes k_1L , and measuring the corresponding beam image on the view screen. The measured two-dimensional beam image was projected along the image's abscissa and ordinate

axes. A Gaussian fitting function is used on each projection to determine the rms value, σ_s in Eq. (2.7). Measurements of σ_s for several quadrupole currents (k_1L) is then fit using the parabolic function in Eq. (2.7) to determine the constants A , B , and C . The emittance (ϵ) and the Twiss parameters (α and β) can be found using Eq. (2.8).

$$\epsilon = \frac{\sqrt{AC}}{l^2}, \quad \beta = \sqrt{\frac{A}{C}}, \quad \alpha = \sqrt{\frac{A}{C}}\left(B + \frac{1}{l}\right). \quad (2.8)$$

2.2.2 The OTR Imaging System

The OTR target is 10 μm thick aluminum foil with a 1.25 inch diameter. The OTR is emitted in a cone shape with the maximum intensity at an angle of $1/\gamma$ with respect to the reflecting angle of the electron beam [14]. Three lenses, 2 inches in diameter, are used for the imaging system to avoid optical distortion at lower electron energies. The focal lengths and position of the lenses are shown in Fig. 2.3. The camera used was a JAI CV-A10GE digital camera with a 767 by 576 pixel area. The camera images were taken by triggering the camera synchronously with the electron gun.

Quadrupole Scanning Experiment

The quadrupole current is changed to alter the strength and direction of the quadrupole magnetic field such that a measurable change in the beam shape is seen by the OTR system. Initially, the beam was steered by the quadrupole indicating that the beam was not entering along the quadrupole's central axis. Several magnetic elements upstream of this quadrupole were adjusted to align the incident electron beam with the quadrupole's central axis. First, the beam current observed by a Faraday cup located at the end of beam line was maximized using upstream steering coils within the linac nearest the gun. Second, the first solenoid nearest the linac gun was used to focus the electron beam on the OTR screen. Steering coils were adjusted to maximize the beam current to the Faraday cup and minimize the deflection of the beam by the solenoid first then by the quadrupole. A second solenoid and the last

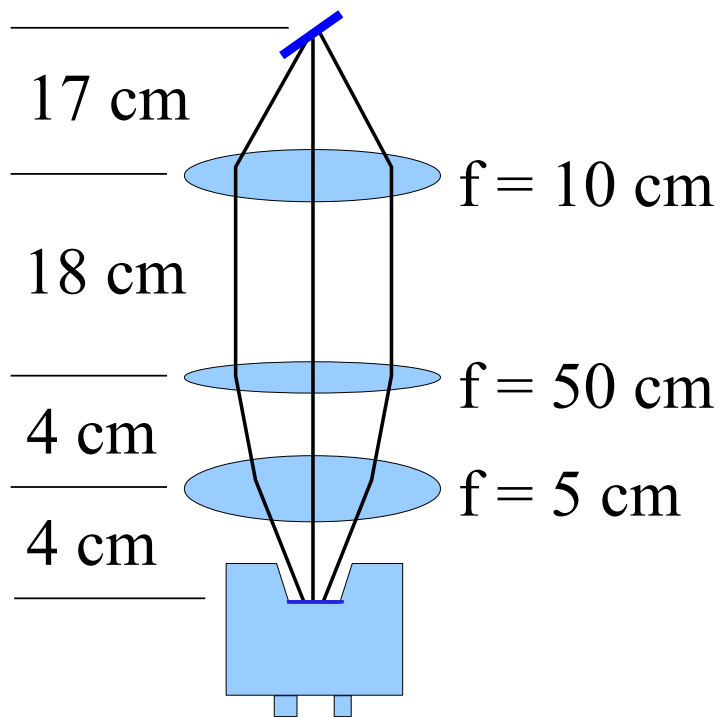


Figure 2.3: The OTR Imaging system.

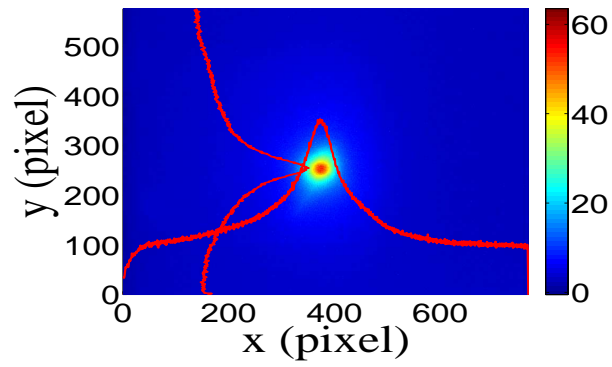
steering magnet, both near the exit of the linac, were used in the final step to optimize the beam spot size on the OTR target and maximize the Faraday cup current. A configuration was found that minimized the electron beam deflection when the quadrupole current was altered during the emittance measurements.

The emittance measurement was performed using an electron beam energy of 15 MeV and a 200 ns long, 40 mA, macro pulse peak current. The current in the first quadrupole after the exit of the linac was changed from -5 A to 5 A with an increment of 0.2 A. Seven measurements were taken at each current step in order to determine the average beam width and the variance. Background measurements were taken by turning the linac's electron gun off while keep the RF on. Background image and beam images before and after background subtraction are shown in Fig. 2.4. A small dark current is visible in Fig. 2.4b that is known to be generated when electrons are pulled off the cavity wall and accelerated.

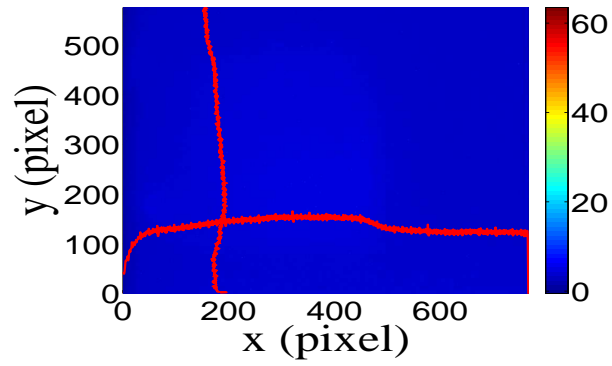
The electron beam energy was measured using a dipole magnet downstream of the quadrupole used for the emittance measurements. Prior to energizing the dipole, the electron micro-pulse bunch charge passing through the dipole was measured using a Faraday cup located approximately 50 cm downstream of the OTR screen. The dipole current was adjusted until a maximum beam current was observed on another Faraday cup located just after the 45 degree exit port of the dipole. A magnetic field map of the dipole suggests that the electron beam energy was 15 ± 1.6 MeV. Future emittance measurements are planned to cover the entire energy range of the linac.

Data Analysis and Results

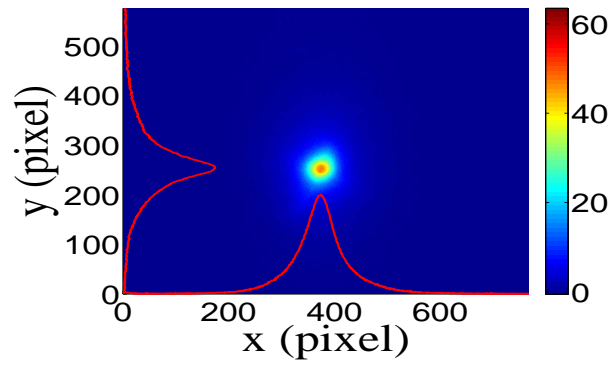
Images from the JAI camera were calibrated using the OTR target frame. An LED was used to illuminate the OTR aluminum frame that has a known inner diameter of 31.75 mm. Image processing software was used to inscribe a circle on the image to measure the circular OTR inner frame in units of pixels. The scaling factor can be obtained by dividing this length with the number of pixels observed. The result is a horizontal scaling factor of 0.04327 ± 0.00016 mm/pixel and vertical scaling factor of 0.04204 ± 0.00018 mm/pixel.



(a)



(b)



(c)

Figure 2.4: Background subtracted to minimize impact of dark current; (a) a beam with the dark current and background noise, (b) a background image, (c) a beam image when dark background was subtracted.

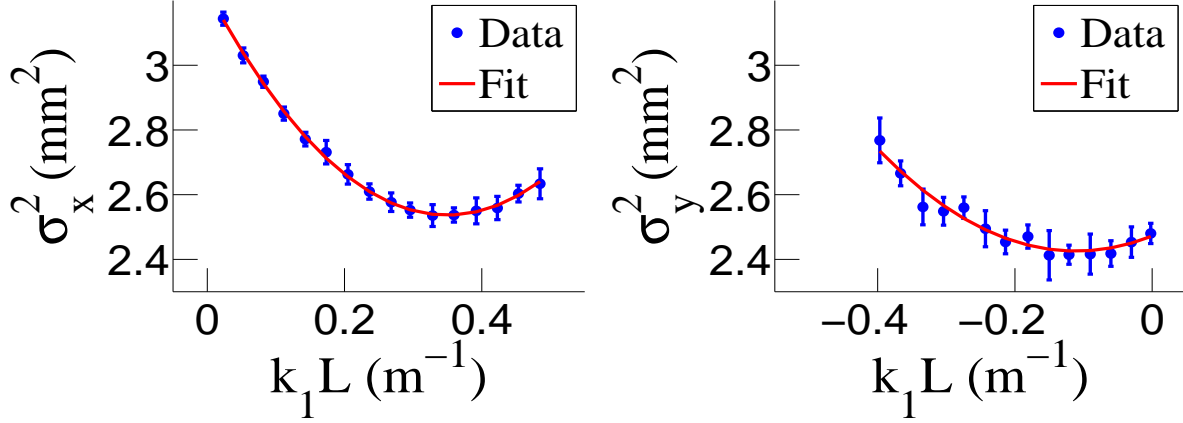


Figure 2.5: Square of rms values and parabolic fittings.

Digital images from the JAI camera were extracted in a matrix format in order to take projections on both axes and perform a Gaussian fit. The observed image profiles were not well described by a single Gaussian distribution. The profiles may be described using a Lorentzian distribution, however, the rms of the Lorentzian function is not defined. The super Gaussian distribution seems to be the best option [19], because rms values may be directly extracted.

Fig. 2.5 shows the square of the rms (σ_s^2) vs k_1L for x (horizontal) and y (vertical) beam projections along with the parabolic fits using Eq. 2.5. The emittances and Twiss parameters from these fits are summarized in Table 2.3.

2.2.3 Conclusions

A diagnostic tool was developed and used to measure the beam emittance of the High Rep Rate Linac at the Idaho Accelerator Center. The tool relied on measuring the images generated by the optical transition radiation of the electron beam on a polished thin aluminum target. The electron beam profile was not described well using a single Gaussian distribution but rather by a super Gaussian or Lorentzian distribution. The larger uncertainties observed for σ_y^2 are still under investigation. The projected emittance of the High Repetition Rate Linac, similar to medical linacs, at ISU was measured to be less than $0.4 \mu\text{m}$

Table 2.3: Emittance Measurement Results.

Parameter	Unit	Value
projected emittance ϵ_x	μm	0.37 ± 0.02
projected emittance ϵ_y	μm	0.30 ± 0.04
β_x -function	m	1.40 ± 0.06
β_y -function	m	1.17 ± 0.13
α_x -function	rad	0.97 ± 0.06
α_y -function	rad	0.24 ± 0.07
micro-pulse charge	pC	11
micro-pulse length	ps	35
energy of the beam E	MeV	15 ± 1.6
relative energy spread $\Delta E/E$	%	10.4

as measured by the OTR based tool described above when accelerating electrons to an energy of 15 MeV. The normalized emittance may be obtained by multiplying the projected emittance by the average relativistic factor γ and β of the electron beam. We plan to perform similar measurements over the energy range of the linac in the near future.

2.3 Energy Scan

Energy scan was done to measure the energy profile of HRRL at nominal 12 MeV. A Faraday cup was placed at the end of the 45 degree beamline to measure the electron beam current bent by the first dipole. Dipole coil current were changed by 1 A increment and the Faraday cup currents were recorded. The relation between dipole current and beam energy is given in the appendix. A 12 MeV peak observed with long low energy tail. The energy distribution of HRRL can be described by two skewed Gaussian fits overlapping [19]. The measurement result and fit are shown in Fig. 2.6 and in Table 2.4

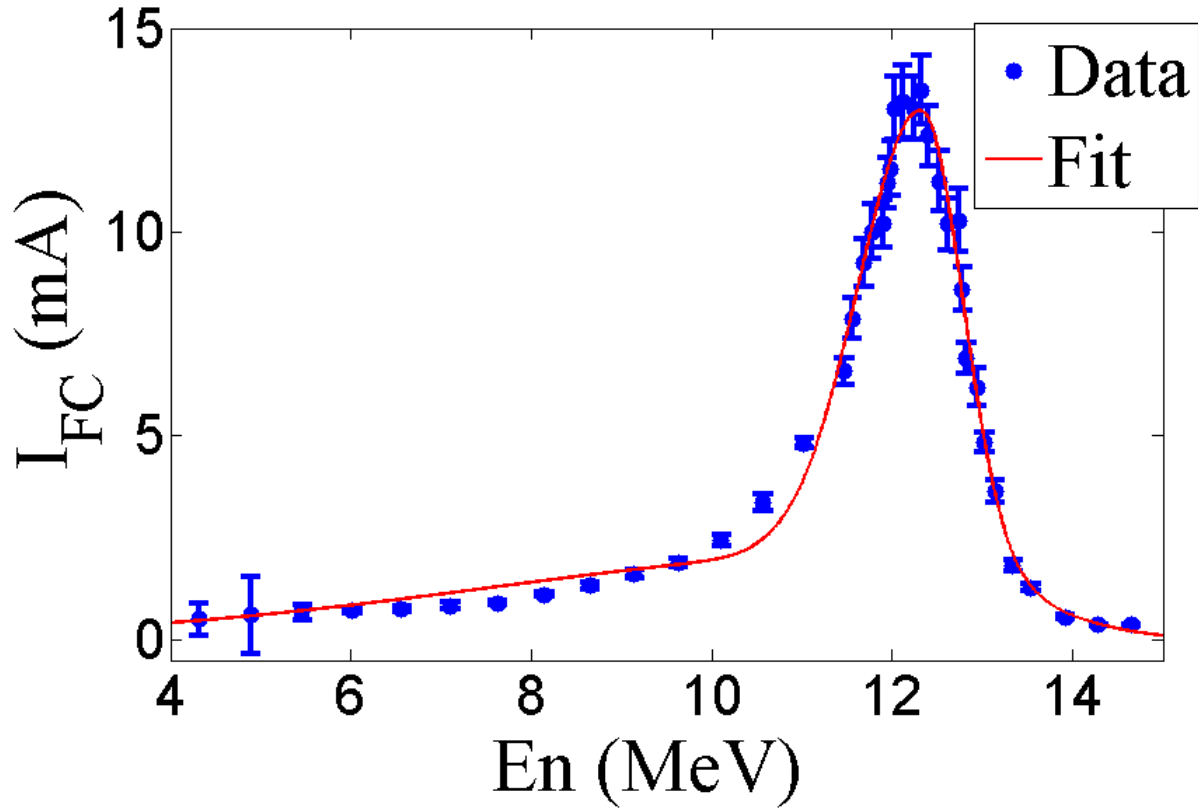


Figure 2.6: HRRL energy scan (blue dots) and fit (red line) with two skewed Gaussian distribution.

Table 2.4: Two Skewed Gaussian Parameters Describes Energy Distribution.

Parameter	Unit	First Gaussian	Second Gaussian
amplitude A		2.14	10.88
mean μ	MeV	12.07	12.32
sigma left σ_L	MeV	4.47	0.70
sigma right σ_R	MeV	1.20	0.45

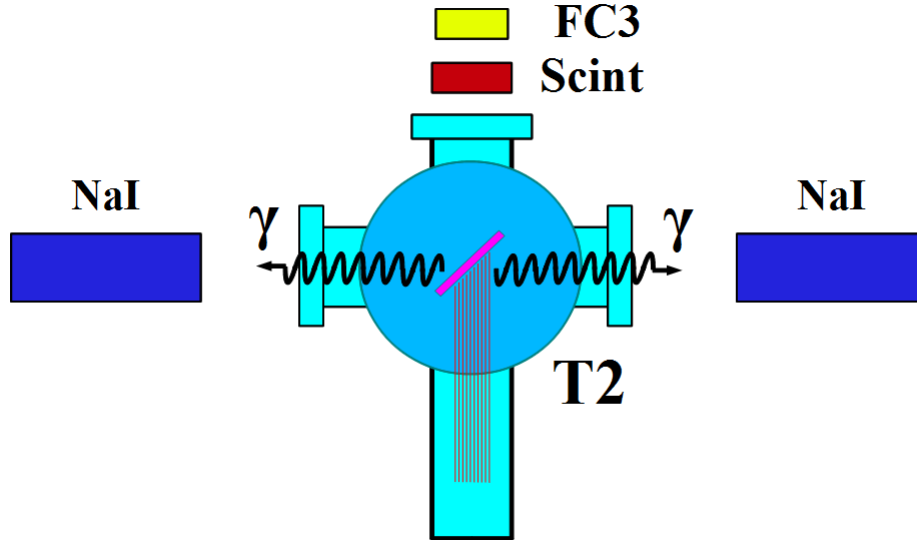


Figure 2.7: Positron Detection System. T2 (pink) is 45 degree placed with horizontal plane, then rotated towards left detector 45 degree.

2.4 Positron Detection

Positrons are transported to the end of the 90 degree beamline, experimental side of the room, which is located at the other side of the wall. A 6-way cross is placed at the end of the beamline to hold T2 and thin windows. 2 NaI detectors are used to detect photons generated during the annihilation process. The setup is shown in Fig. 2.7. There are also a scintillator and a Faraday cup at the end of the beam tuning purposes. Most of the positrons reach T2 first thermalized inside and then annihilates. As they thermalize they lose their kinetic energy and photon energy emitted in annihilation is rest mass energy of electron, 511 keV. Two photons radiated back-to-back isotropically during the annihilation process. Two NaI detectors are in coincidence mode with short time window (tens of ns) to eliminate noises. Only when two photons happened to be in the incident in short time window, the signals are recorded as one entry.

Table 2.5: Radioactive sources and photon peaks.

Radioactive Sources	Unit	First Peak	Second Peak
Co-60	keV	1173	1332
Na-22	keV	511	1275

2.4.1 NaI Detectors

NaI crystals, shown as in Fig. 2.9, acquired from IAC were used to detect 511 keV photons from positron annihilation. Since the detectors had pulse length around 400 μ s, the PMT bases were redesigned and rebuilt. The NaI detectors have two outputs, one is at second last dynode and one anode signal. PMT base configuration of the NaI detectors is shown in the Fig. 2.8 and bases made shown in Fig. 2.10. It takes ADC 5.7 μ s to convert analog signal to digital signal. The signal from anode was delayed 6 μ s by long cable and sent to the ADC. PMT base take HV around -1150 V.

Rebuilt PMT bases because old base pulse length is around 400 μ s. The new base pulse length around 1 μ s. The NaI crystal is SAINT-GOBAIN CRYSTAL & DETECTORS (MOD. 3M3/3) with sizes of 3x3. Bases were calibrated using Na-22 and Co-60 sources with photon peaks indicated in the Table 2.5.

2.4.2 Trigger for DAQ

The trigger for DAQ required a coincidence between one or more NaI detectors and the electron accelerator gun pulse. The last dynode signals from left and right NaI detectors were inverted using a Ortec 474 amplifier and sent to a Constant Fraction Discriminator (CFD Model specs). RF noise from the accelerator is as large as the signal from the NaI detector. Since it is correlated in time with the gun pulse, the gun pulse was used to generate a VETO pulse that prevent the CFD from triggering on this RF noise. After this discrimination and RF noise rejection, the discriminated dynode signals were sent to an Octalgate Generator (Model) that increased the width of the logic signals to prevent multiple pulses during a single electron pulse. Then the signals were sent to Quad Coincidence to generate AND

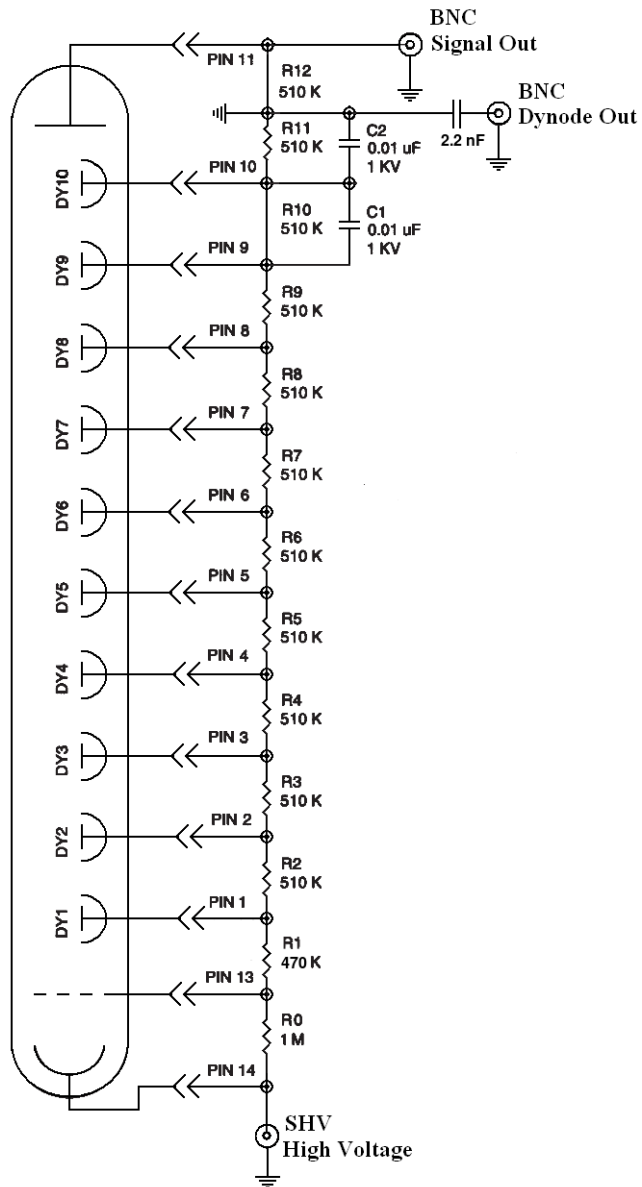
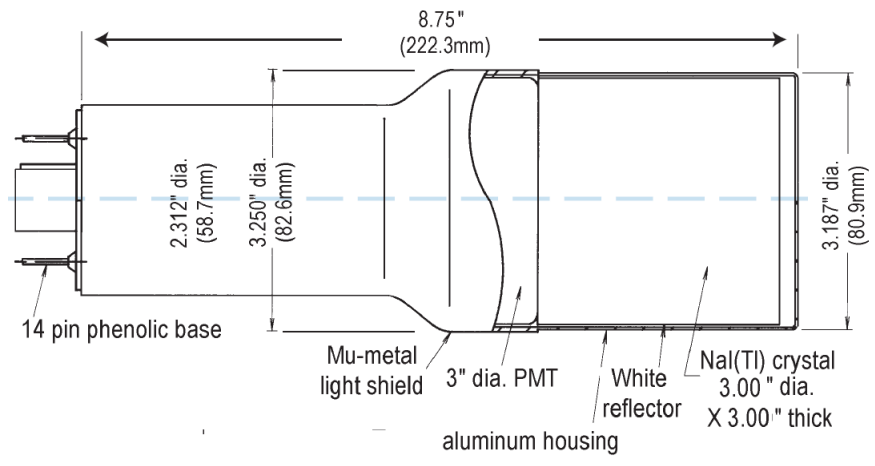


Figure 2.8: Modified PMT base design.



Model 3M3/3

Figure 2.9: NaI crystal dimension.



Figure 2.10: NaI crystals and new bases.

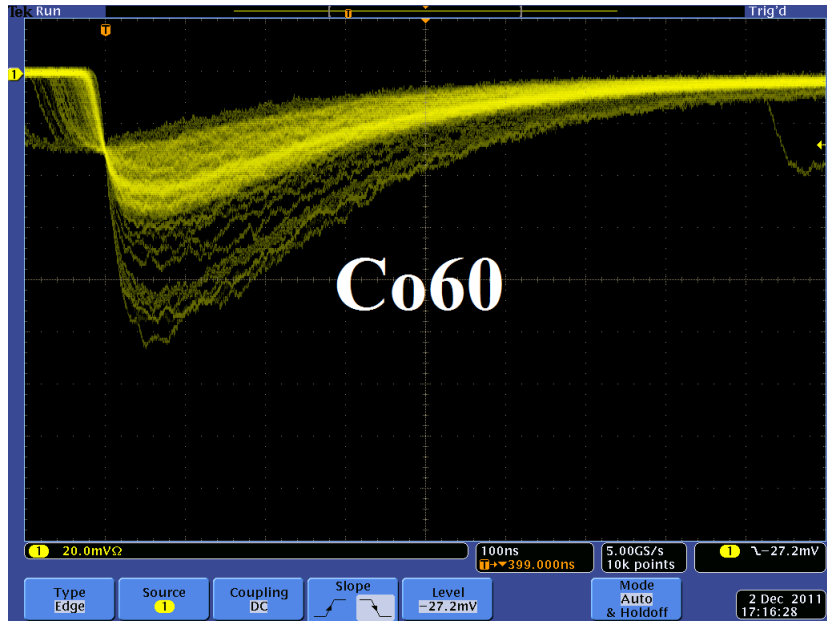


Figure 2.11: Pulses from Co-60 source observed on the scope. The amplitude is about 60 mV. The rise time is larger than 50 ns, and the fall time is larger than 700 ns.

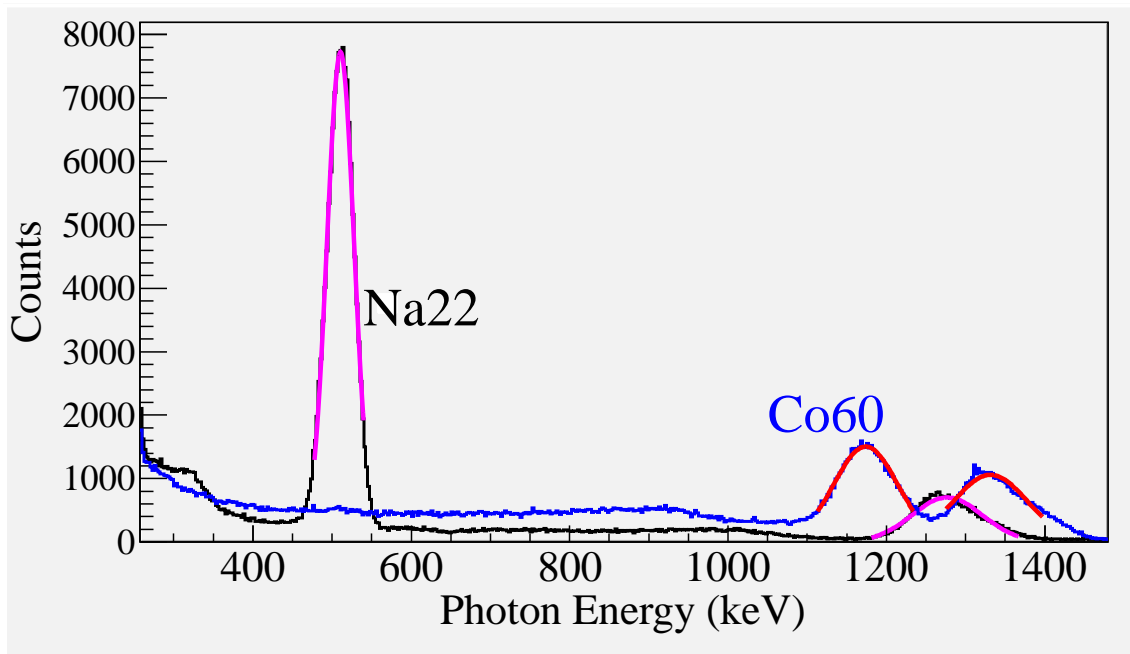


Figure 2.12: Calibrated NaI spectrum of Na-22 and Co-60 sources.

logic between electron gun and dynode signals. The logic is set as:

$$(NaI\ Left \ \&\& \ Gun\ Trigger) \ \&\& \ (NaI\ Rgiht \ \&\& \ Gun\ Trigger). \quad (2.9)$$

This is to make sure we have trigger when photons back to back scatter to the NaI detectors when electron gun is on. Then this trigger was sent to ORTEC Gate & Delay Generator. One of the out from gate generator was used to generate a gate to read analog signal from anode. Another output was delayed by 6 μ s, necessary time to convert the analog signal from anode to digital signal, and used as trigger for the DAQ.

== Simulation ==

Chapter 3

Simulation

A simulation was performed using the package G4beamline(ref Muons inc) to study the processes of position generation and transportation. "G4beamline is a particle tracking and simulation program based on the Geant4 (reference G4) toolkit that is specifically designed to easily simulate beamlines and other systems using single-particle tracking." Since the ratio of e^+/e^- during the positron generation process is very low (on the order of 0.001) and the positron beam loss during the transportation is large, it was necessary to divide whole process into 5 steps. A new beam event generator is created based on the results of the previous step in the simulation. The first step generates electrons according to a measurement made of the accelerator that was used in the experiment. Electrons are transported to T1 in vacuum and as a result the interactions of the electron with T1 produce positrons. The second step is the transportation of the positrons generated at T1 to the entrance of first dipole magnet. The third step is the transportation of the positrons from the entrance of the first dipole magnet to the end of the second dipole. The fourth step is the transportation of the beam from the exit of the second dipole to the T2 target. The fifth step is the positron beam interaction with T2 and detection of the resulting 511 keV photons.

3.1 Step 1 - The Electron Beam Generation and Transportation to T1

In this step, an electron beam is generated from the experimental measure electron beam parameters. The Twis parameters described in the earlier chapter used electron generated

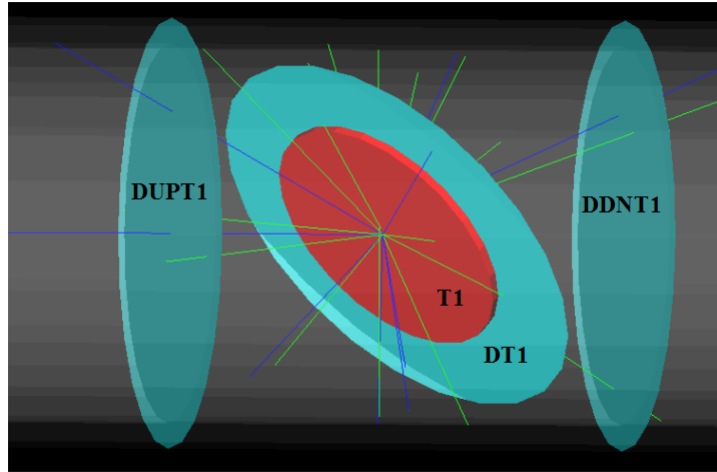


Figure 3.1: T1 is positron production target with same geometry and material as real target. DUPT1 is virtual detector located upstream to sample incoming electron beam. DDNT1 is down stream virtual detector; DT1 is a virtual detector that is placed right after T1 with same angle as T1.

the beam. The energy distribution of the beam is measured and shown in the Fig. 2.6. The blue dots are measurements and red line are the fit composed of two skewed Gaussian distributions. The fit parameters are given in the Table 2.4 in the previous chapter.

Series of virtual detectors are placed along the beamline to sample the beam. As an example, in the Fig. 3.1 shown are three detectors and the T1. The electron beam is observed at DUPT1 (Detector 25.52 mm UPstream of T1) and positrons (or electrons and photons) generated during the interaction of electron beam with T1 are observed at DT1 (Detector of T1) and DDNT1 (detector Down 25.52 mm stream of T1).

3.1.1 Positron Beam on DDNT1

13,799,743,900 electrons were shot on T1 and resulted positron beam observed at DDNT1 is as shown below Figures. Fig. 3.2 shows transverse positron spacial and angular distribution on the DDNT1. The transverse spacial and angular

As can be seen on Fig 3.3 (b) and (c) The y spacial distribution and y divergence dis-

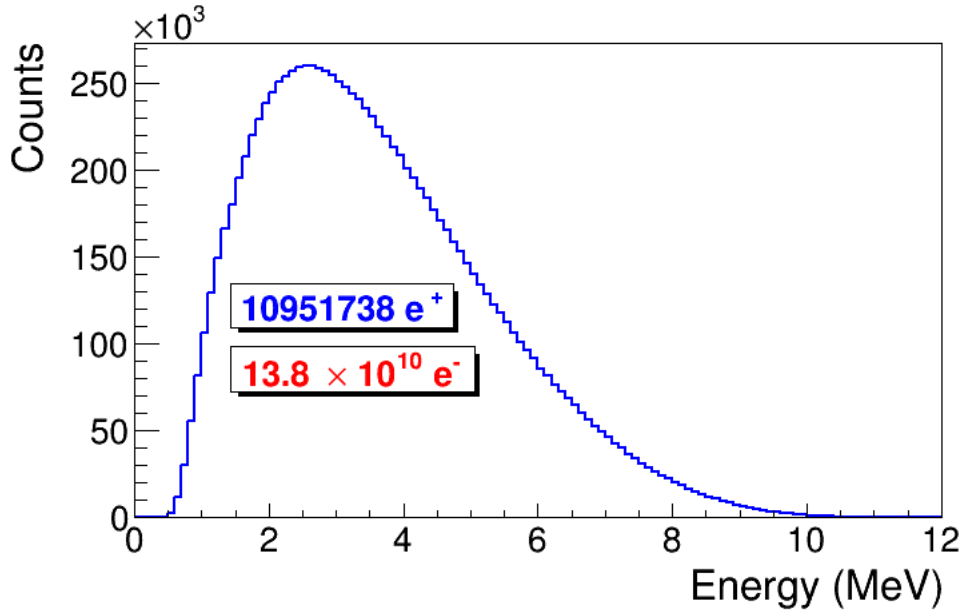
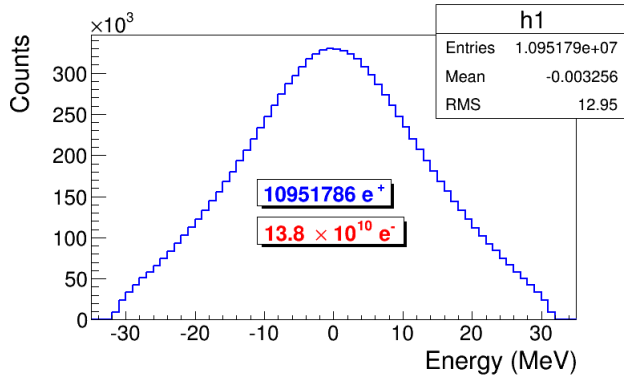


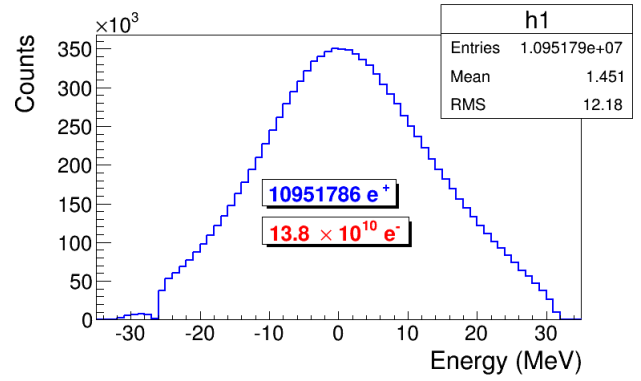
Figure 3.2: Energy distribution of positrons detected on virtual detector DDNT1.

tribution of the beam has sharp drops on their left side. The y vs. x distribution of the beam shown in Fig. 3.3 (e) and Fig. 3.3 (f) is zoomed in version of 3.3 (e). has a sharp drop in the region between -25.8 mm and -27.2 mm that corresponds to the boundary of the target T1. Fig. 3.4 shows the geometry of the target T1 and the sensitive detector DDNT1. If the target size was increased, it would eventually intersected the detector DDNT1 at a distance of 25.8 mm from the beam center. A 1.4 mm wide stripe of low counts is visible on DDNT1 that is a result of the target's thickness of 1.016 mm and the 45° angle of intersection ($1.016\sqrt{2} = 1.44$). The edge of the target does not produce many positrons compared to the face of the target, and as a result you see the stripe.

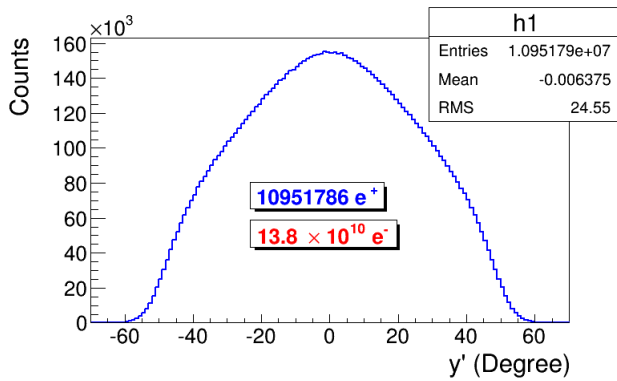
As shown in Figs. 3.5 (a) and (b), the spacial distribution on Y decrease occurs at $= 45^\circ$. Positrons are emitted from both the downstream and upstream side of the target. As shown in the figure, positrons from the downstream side of the target intersect the detector at angles below 45 degrees while positrons from the upstream side of the target begin to hit the detector at angles beyond 45 degrees. The 1.4 mm gap represents the transition of positrons between these two extremes.



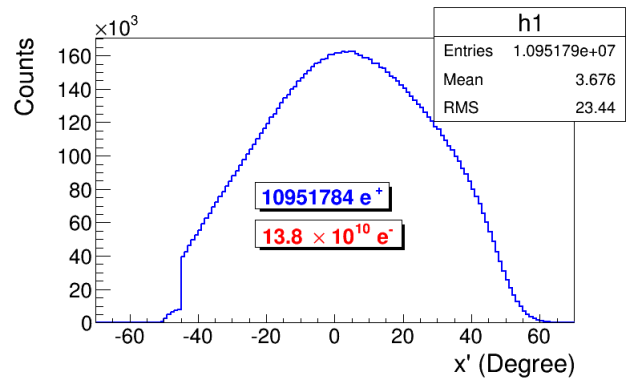
(a) X DDNT1



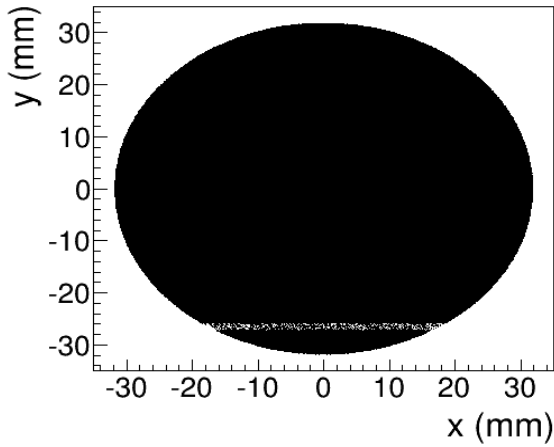
(b) Y DDNT1



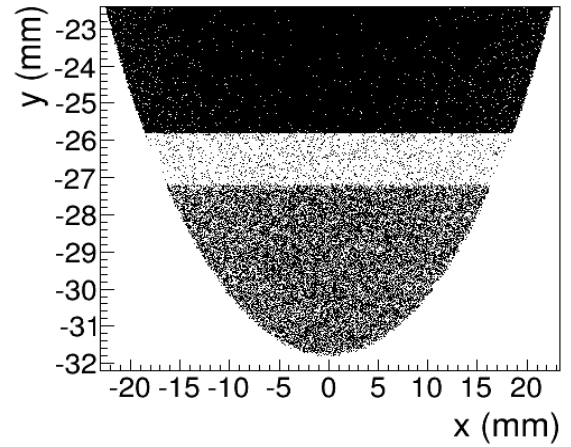
(c) X' DDNT1



(d) Y' DDNT1



(e) X vs. Y DDNT1



(f) X vs. Y DDNT1 zoom

Figure 3.3: Transverse spacial and angular distribution of positrons on the virtual detector DDNT1.

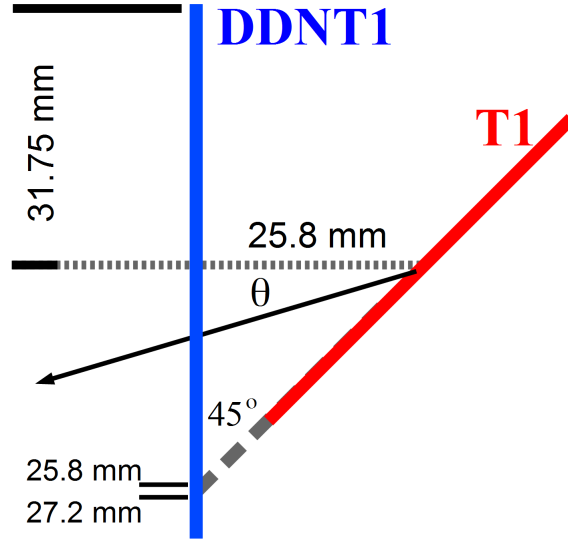


Figure 3.4: Geometry of the target T1 and the virtual detector DDNT1.

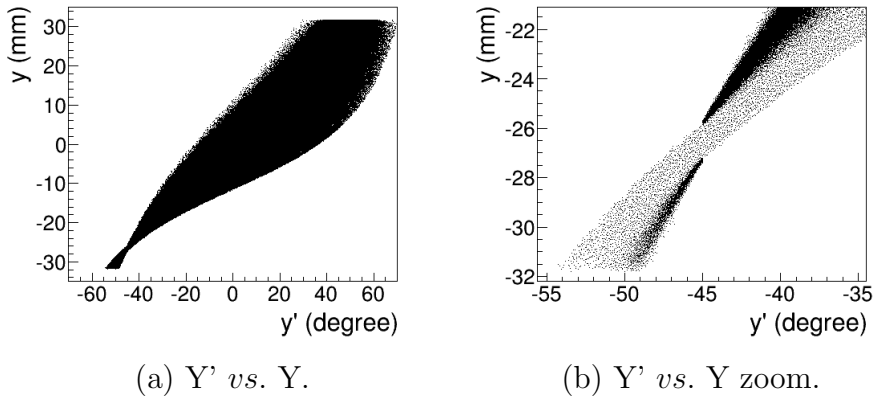


Figure 3.5: Positron beam distribution Y divergence vs. Y spatial distribution on DDNT1.

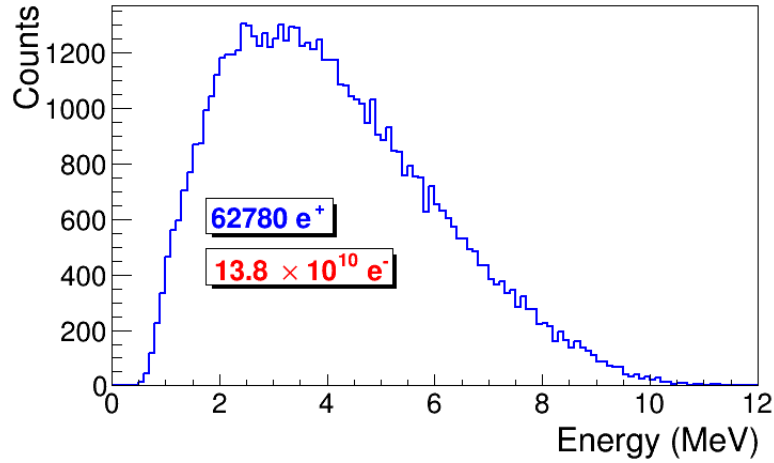


Figure 3.6: e^+ Energy on DQ4

3.1.2 Positron Beam on DQ4 and DD1

Resulted positron beam on DQ1 and DD1 are shown in below Figures.

3.2 Step 2 - Transportation of the The Positron Beam after T1 to The Entrance of The First Dipole

In this step, the positrons generated in the first step divided into 1 keV/c momentum bins and each bin is sampled individually since the momentum of the positrons related to their divergence. Multiple beams with individual weights generated at downstream T1 detector DDNT1 and transported to entrance of the D1. Virtual detectors are placed at the entrance of Q4 and entrance of D1 to track positrons and generate beam for next step as shown in the Fig 3.8.

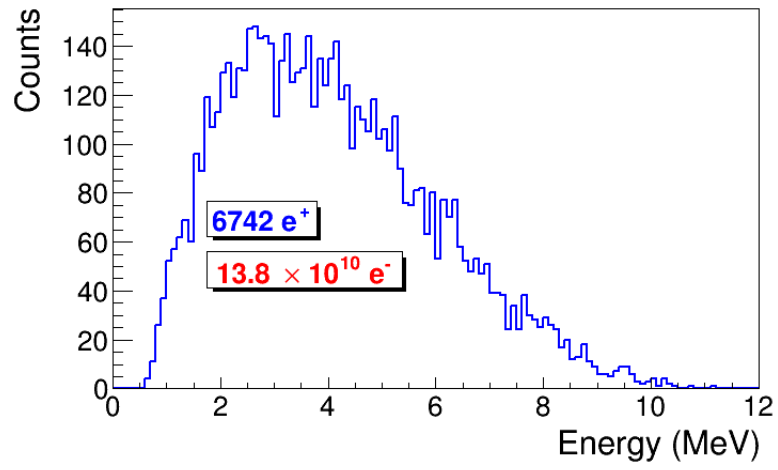


Figure 3.7: e^+ Energy on DD1

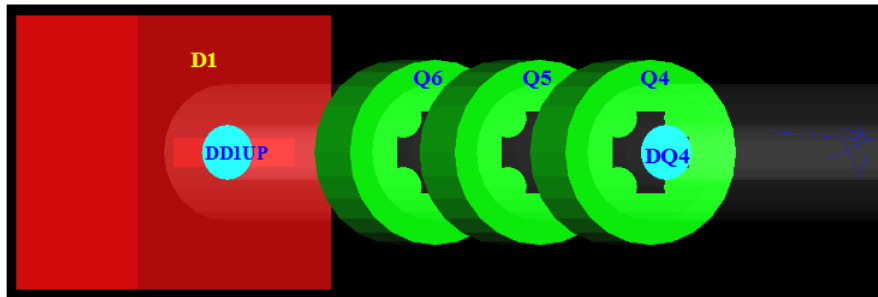


Figure 3.8: Step 2 setup.

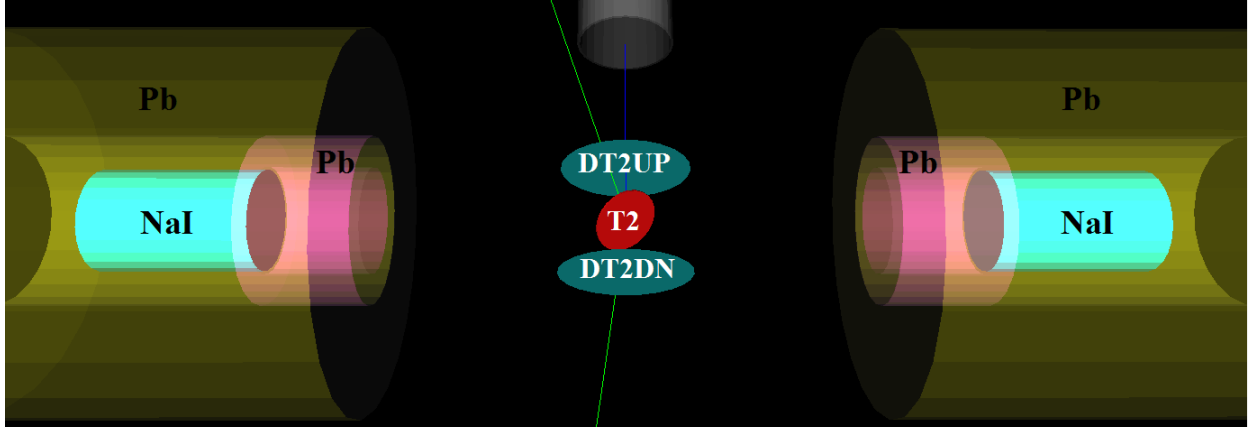


Figure 3.9: T2 and virtual detectors located upstream (DT2UP) and downstream (DT2DN) of T2. NaI detectors and Pb shielding.

3.3 Step 3 - Generation of Positrons at the Entrance of the First Dipole and Their Transporting and Detection

In this step, positrons are generated at the entrance of the first dipole (as shown DD1UP shown in Fig. 3.8) by sampling the beam at the same location in previous step. Beam then transported down to T2 located at the end the beamline as shown in Fig. 3.9.

3.3.1 Transport Efficiency

In this step, 14,359,380,000 positrons generated at DD1. By using the DQ4 and DDNT1 to DD1 ratios of we obtained from previous two steps, one can calculate that it is equivalent generating 57,559,974,511,209.3 at DDNT1, and detecting 375,891,831,521 at DQ4 and 14,359,380,000 at DD1 (i.e. $DDNT1:57,559,974,511,209.3 \text{ ; } DQ4:375,891,831,521 \text{ ; } DD1:14,359,380,000$). The transported positrons detected at the end of the beamline by DT2UP. The beam lost is shown in Table and Fig.

Table 3.1: Transportation Efficiency

Energy (MeV)	Generated at T1	Entered Q4	Entered D1	Reaches T2	NaI Detectors in Coincidence
1.015 ± 0.25	2.52888×10^{12}	1.36481×10^{10}	1.3676×10^9	1.0707×10^4	6
1.5 ± 0.25	4.91629×10^{12}	2.74778×10^{10}	2.75965×10^9	140228×10^5	53
2.15 ± 0.25	6.47248×10^{12}	3.75594×10^{10}	3.76997×10^9	9.5808×10^6	477
2.5 ± 0.25	6.79791×10^{12}	4.05435×10^{10}	4.06923×10^9	1.1902×10^6	517
3 ± 0.25	6.63138×10^{12}	4.06935×10^{10}	4.08565×10^9	1.19604×10^6	488
3.5 ± 0.25	6.11215×10^{12}	3.88598×10^{10}	3.89856×10^9	1.1938×10^6	474
4.02 ± 0.25	5.34016×10^{12}	3.50619×10^{10}	3.5211×10^9	1.15945×10^6	472
4.5 ± 0.25	4.5764×10^{12}	3.09881×10^{10}	3.10839×10^9	1.09549×10^6	444
5 ± 0.25	3.769×10^{12}	2.65371×10^{10}	2.66784×10^9	1.01029×10^6	392
5.5 ± 0.25	3.01205×10^{12}	2.20521×10^{10}	2.21408×10^9	9.06707×10^5	354

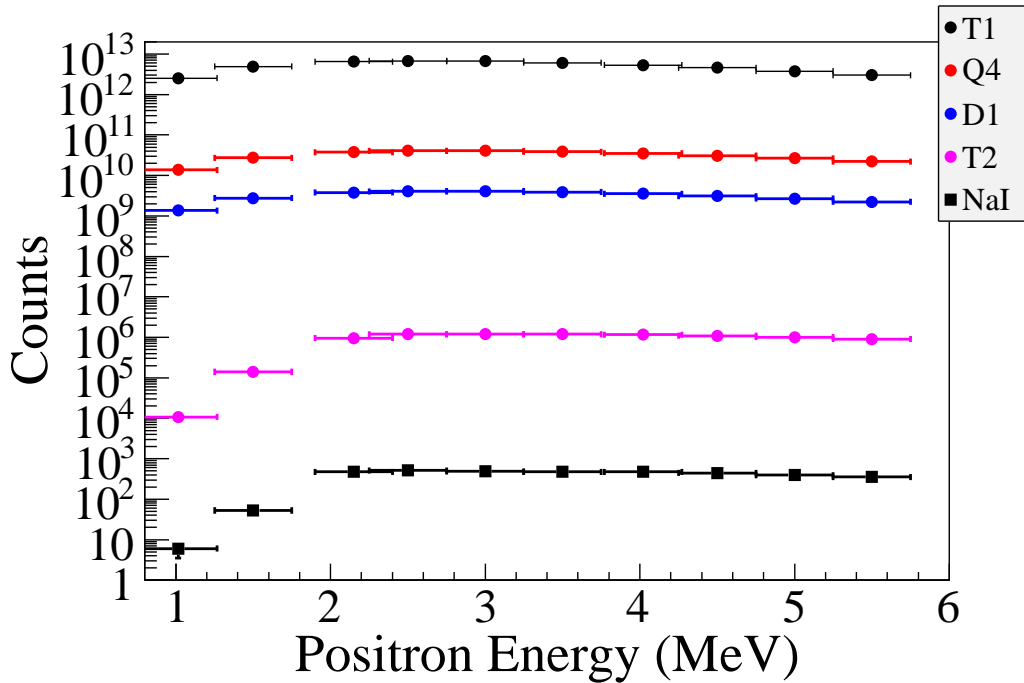


Figure 3.10: Beam loss during transportation.

3.3.2 Detector efficiency

According to the detector efficiency chart, shown in Fig. 3.11 obtained from SAINT-GOBIAN CRYSTALS [21], at 511 keV, NaI crystals have 68% efficiency. If they are in coincidence, their efficiency is $68\% * 68\% = 46.24\%$.

3.4 Quadrupole Triplet Collection Efficiency Study

Quadrupole triplet positron collection and transportation efficiency was studied by regenerating positrons after T1. Several quadrupole current settings were simulated and shown in Table 3.2. 5475869400 positrons were generated and transported to the entrance of the D1, first dipole. A virtual detector is located at the entrance of the D1 to study collection and transportation efficiency of the triplet system. As it can be seen from the table, for different quadrupole settings, there are not any significant differences in the number of positrons and their

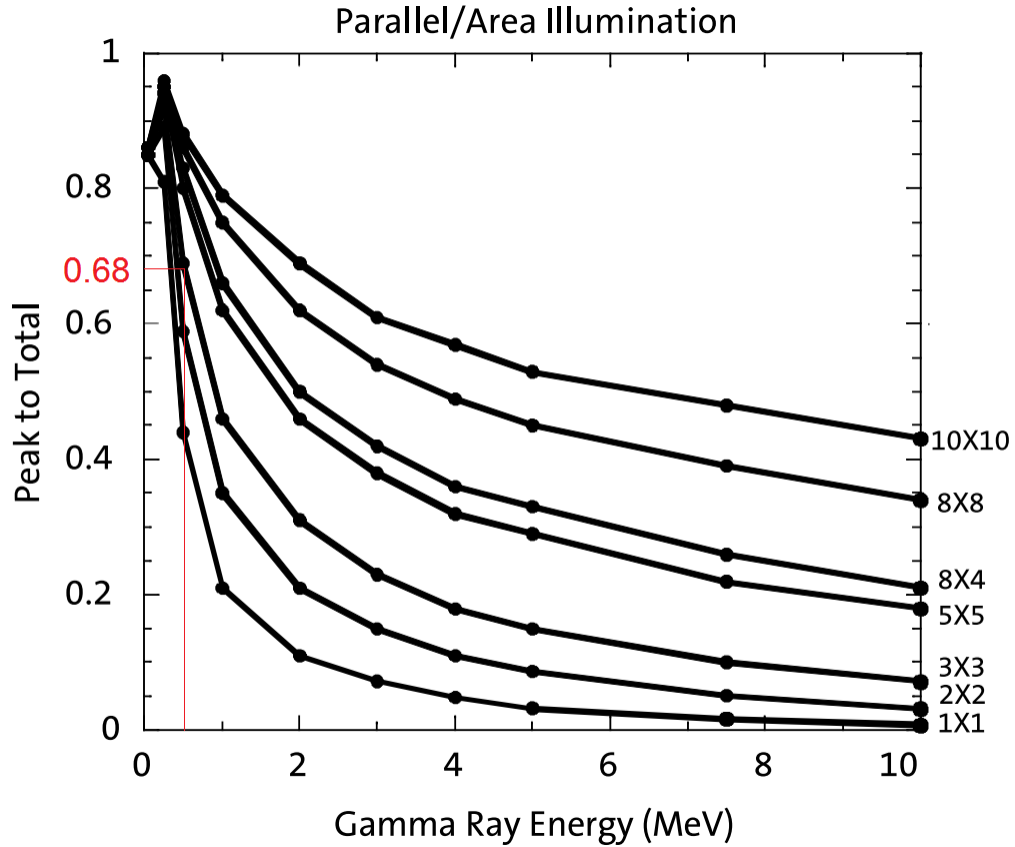


Figure 3.11: NaI detector efficiency [21].

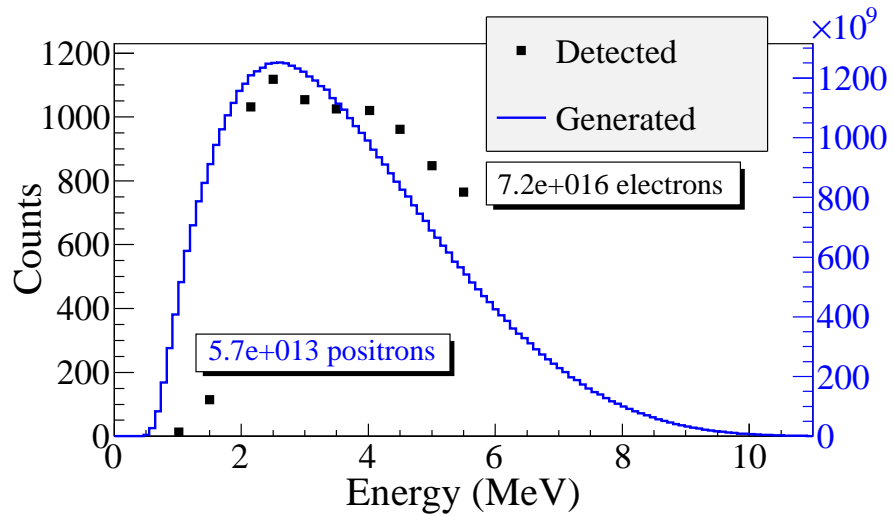


Figure 3.12: Positrons generated detected on virtual detector DDNT1 and 511 keV counts detected by NaI detectors in coincidence mode (100 % efficiency assumed).

position and momentum distributions. On average, 3590413 positrons entered D1. The ratio of positrons generated to the ones enter D1 is 1525:1.

Table 3.2: Quadrupole Triplet System Collection and Transportation Efficiency Study.

Q4	Q5	Q6	Entries	x	σ_x	y	σ_y	Px	σ_{Px}	Py	σ_{Py}	Pz	σ_{Pz}
-1	2	-1	3587220	-0.004534	12	0.03058	12	3.019e-05	0.04613	-0.002159	0.04553	3.848	1.875
-2	4	-2	3591423	-0.01223	12	0.04902	12	2.187e-05	0.04612	-0.002109	0.04554	3.848	1.875
1	-2	1	3591509	-0.009171	12	0.04015	12	-1.493e-05	0.04616	-0.002154	0.04557	3.849	1.876
1	2	1	3589854	-0.005396	12	0.03384	12	-1.779e-05	0.04615	-0.002156	0.04556	3.849	1.876
2	-4	2	3592977	-0.007413	12	0.03225	12	-3.261e-06	0.04615	-0.002173	0.04549	3.849	1.876
2	4	2	3589495	-0.004142	12	0.03271	12	3.042e-06	0.04616	-0.002183	0.04554	3.849	1.875

== Experiment ==

Chapter 4

Experiment

4.1 Runs

The annihilation target T2 is can be inserted or removed from the center of the beamline. This allow two kind runs, T2 in and T2 out. When T2 is in the positions are delivered to T2 and thermalize and annihilate produces 511 KeV photons. This photons are detected by the NaI detectors as shown in Fig. 4.1. When T2 is out, positrons exits beamlien and transported to the beam dump. NaI detectors are shielded with Pb bricks from the beam dump. T2 out runs serve as background measurements.

T2 is placed inside a 6-way cross and two horizontal side it sealed with thin windows. Two NaI detectors placed horizontally to T2, perpendicular to the 90 degree beamline and pointed to this windows. The spectrum taken with T2 in and out are shown in the Fig. 4.2.

Run No. 3735 (T2 in) and run No. 3736 (T2 out) in the Fig. 4.2, the two sub-figures acquired by cut that only incidents happened in 511 keV peak coincidently on both detectors. The positron counts extracted by subtracting background (blue in figure) and integrating the peak. The integral shown in red is from the background is subtracted spectrum. The

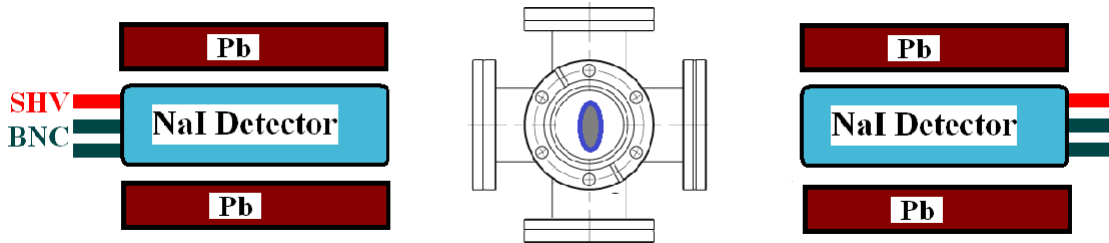
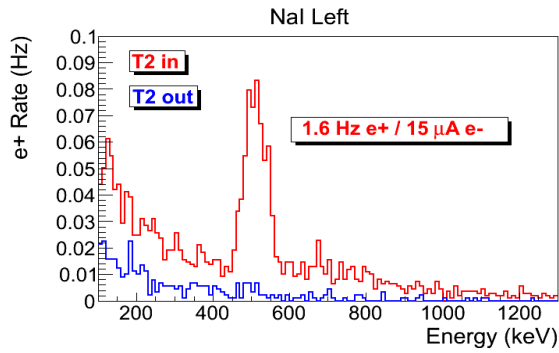
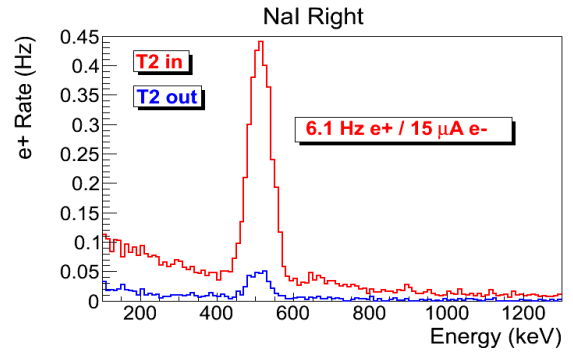


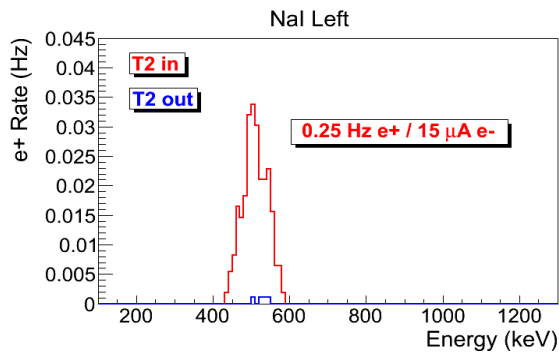
Figure 4.1: Positron detection using T2 and NaI detectors.



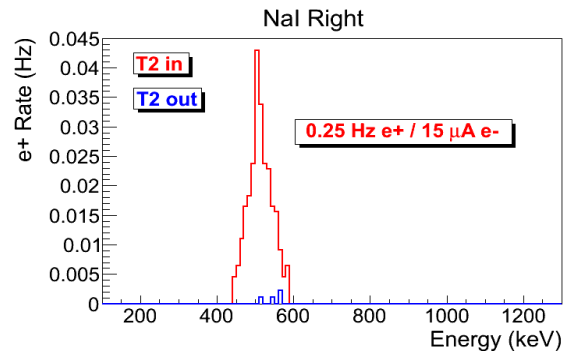
(a) Original spectrum on left NaI.



(b) Original spectrum on right NaI.



(c) Spectrum with cut on left NaI.



(d) Spectrum with cut on right NaI.

Figure 4.2: T2 in run (red) and T2 out background run (blue) time normalized spectrum. Top row shows original spectrum and bottom row shows incidents only happen in 511 keV peak coincidentally on both detectors.

Table 4.1: Run Parameters of Run No. 3735.

Parameter	Unit	Value
run number		3735
repetition rate	Hz	300
run time	s	1002
pulses		301462
events		9045
e+ Counts NaI Detectors		256 ± 16

Table 4.2: Scintillator Calibration Data.

Run Number	Faraday Cup Charge Area (nVs)	Mean of ADC Channel 9
3703	1201 ± 10	1126 ± 0.8
3705	777 ± 110	791.8 ± 0.6
3706	367.7 ± 2.3	242.1 ± 0.3

run parameters of Run No. 3735 is given in Table. 4.1

4.2 Electron Current Estimation

A photon scintillator was placed between quadrupole 9 and quadrupole 10 shown as in the Fig. 4.3 and used as electron beam monitor. To calibrate this scintillator electron beam changed incrementally and the charge was measured both on oscilloscope and ADC. As the electron beam increases the beam charge observed on the scope increased and the photon peak in the ADC also shifted towards right end of the spectrum. The measured results are shown in the Table 4.2. The result shows that the relation between electron beam current and scintillator ADC channel number is linear, $(0.93 \pm 0.14)/50$ nVs/(ADC channel number). The spectrum taken is shown in Fig 4.4.

To find the average charge in a run two methods were used. One method calculates

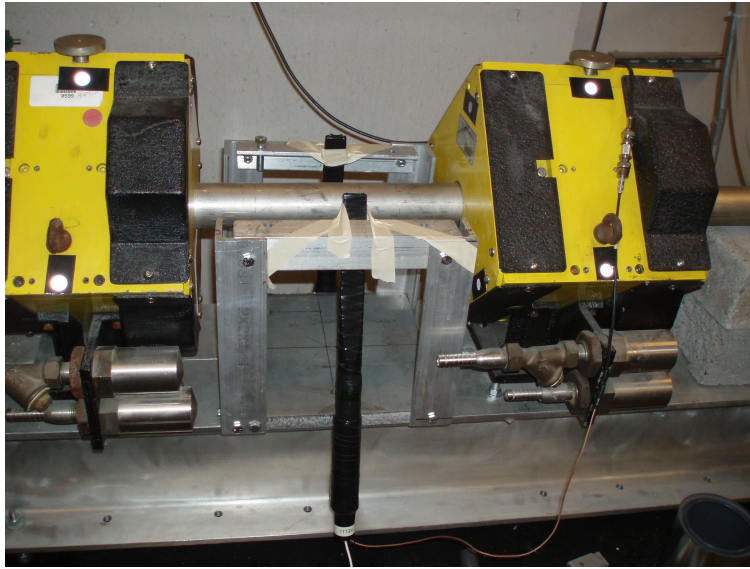


Figure 4.3: Electron beam monitor.

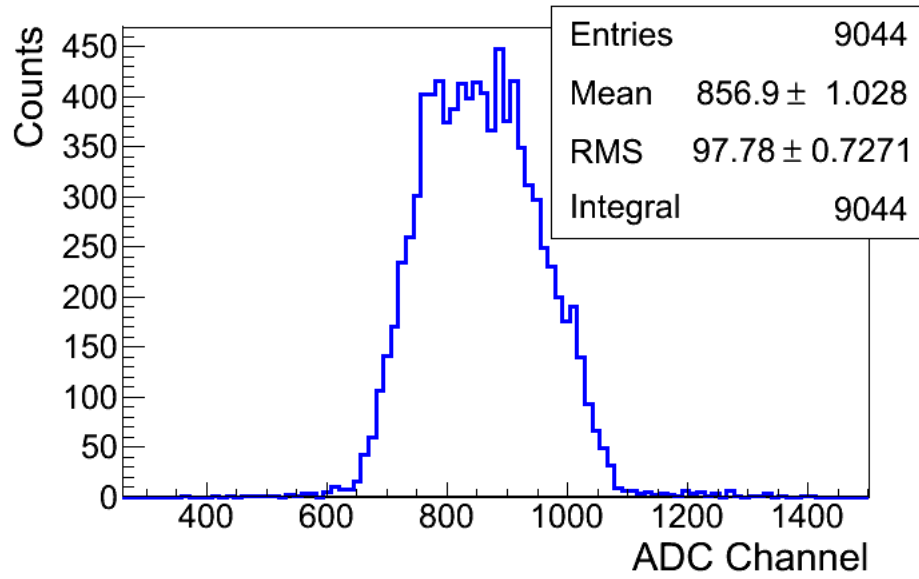


Figure 4.4: Electron beam monitor ADC signal

charge bin by bin and add up charges in all the bins as shown in Eq. 4.1

$$Q_{e^-} = \sum_i i \times (\text{bin content}[i]) \times Q_{Calb} \times (\text{pulses/events}). \quad (4.1)$$

In another method, the mean of the of the spectrum multiplied with total number of pulses in the run as shown in Eq. 4.2. Of course the calibration factors multiplied in both methods. The average of the two methods is taken.

$$Q_{e^-} = (\text{Mean ADC Channel Number}) \times (\text{pulses}) \times Q_{Calb}. \quad (4.2)$$

For example, the average of the two in run 3735 is $(4.8 \pm 0.5) \times 10^{-3} C.$. Then this total charge can be used to calculate total numbers of the electrons or average current of electron beam in this run.

4.3 Positron Current Estimation

Fig. 4.3 are the background subtracted spectrum. The (a) and (b) are NaI left and right detectors' spectrum. The (c) and (d) are NaI left and right detectors' spectrum with cut around 511 keV peak and after requiring coincident event on both detectors.

4.3.1 Positron to Electron Ratio

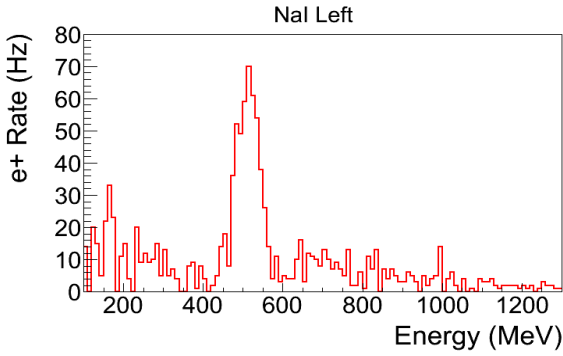
The measured ratio of positron to electron ratio is given the following Table 4.5 and Fig. 4.5.

4.3.2 Sources of Systematic Errors

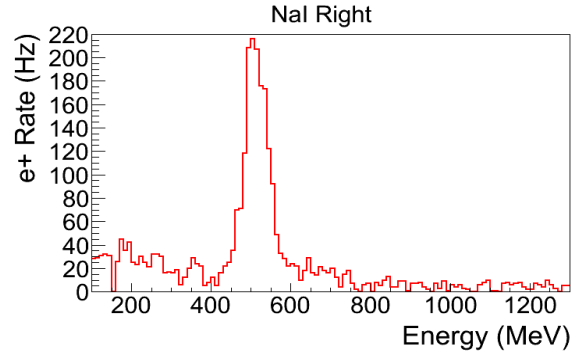
Error on Energy

To find Error on the energy, the electron beam is directed to the phosphorous screen at the end of the 90 degree beamline. The beam centered then steering away from the center.

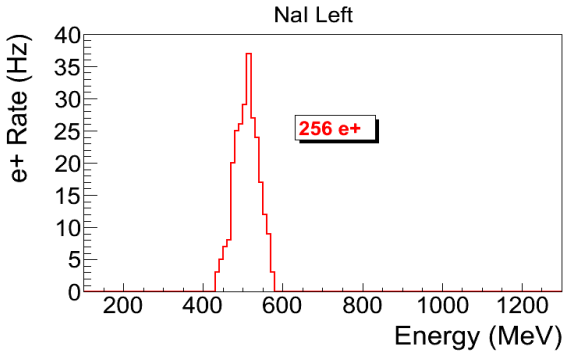
Table 4.3: Run 3735



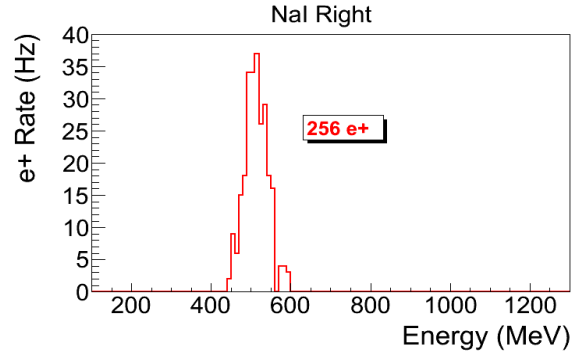
(a) Left NaI



(b) Right NaI



(c) Left NaI with cut and coincidence



(d) Right NaI with cut and coincidence

Table 4.4: NaI positron run spectrum.

Table 4.5: Run 3735

Energy	Positron to Electron Ratio
1.02 ± 0.13	$(0.19 \pm 0.19) \times 10^{-16}$
2.15 ± 0.13	$(0.69 \pm 0.24) \times 10^{-16}$
3.00 ± 0.13	$(8.25 \pm 0.96) \times 10^{-15}$
4.02 ± 0.13	$(4.20 \pm 0.80) \times 10^{-15}$
5.00 ± 0.13	$(0.62 \pm 0.16) \times 10^{-16}$

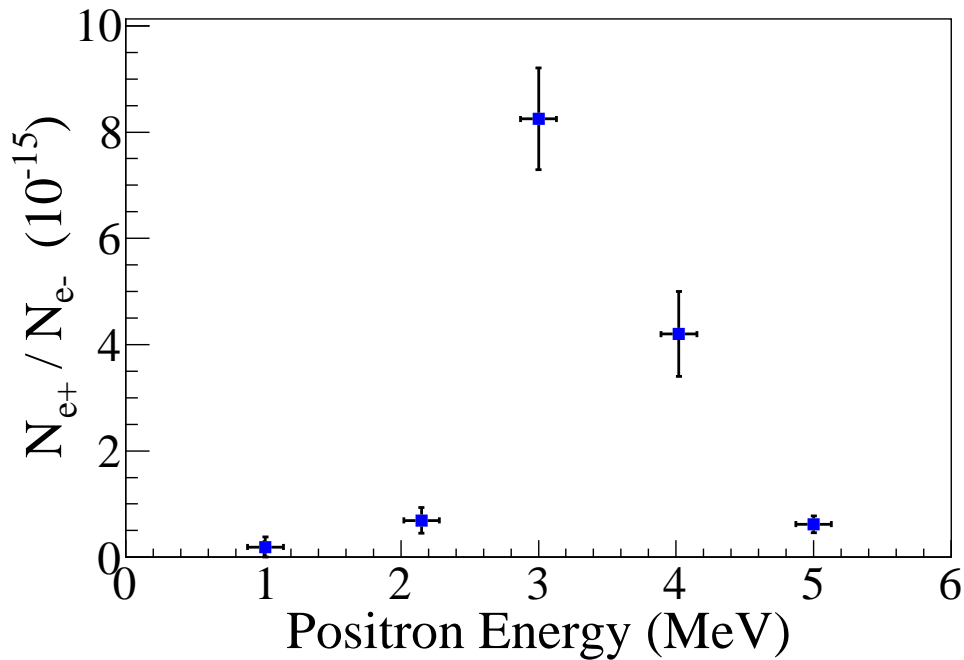


Figure 4.5: Ratio of positrons detected to electrons in experiment.

The current change on the dipole I when beam is center and at the edge is 0.2 A. This is corresponding to 0.13 MeV in beam energy.

Error on Ratio

Error on electron beam is derived from:

Error on positron beam rate is derived from: $\sqrt{\frac{\text{positron rate}}{\text{run time}}}$

Annihilation Target Angle

Use simulation to determine how sensitive annihilation of positrons is to angle.

What is the dependence of the annihilation target angle with the probability of a positron annihilating in the target and producing a photon that is detected by the NaI detector,

What is the distribution of 511s as a function of angle phi when theta is 90 degrees? Are they uniformly produced?

Energy cut systematics

How does the positron production efficiency change when you change the range of the 511 cut.

= Conclusions and Suggestions =

Chapter 5

Conclusions and Suggestions

1. HRRL beamline: The HRRL cavity placed to new location. New magnetic elements and diagnostic tools added to the beamline. HRRL beam successfully reconfigured for positron production and can also generate electron beam with improved quality.

2. Successfully constructed a positron detection system using two NaI detectors, thin tungsten foils a 6-way cross.

3. Successfully measured positrons at different energies (1 – 5 MeV) in experiment. Production efficiency ($e^+ : e^-$ ratio) is on the order of 10^{-15} and peak distribution observed around 3 MeV.

4. In the experiment quadrupoles were optimized to transport 2 MeV due to the limited beam time and it could have diminished transportation efficiency for other energies. Further experimental study is necessary to investigate the positron beam energy distribution.

5. Simulation results indicate that the transportation efficiency are different for different energies. Higher energies has higher transportation efficiency. While simulation results agrees with experiment in the peak energy distribution is around 3 MeV, it disagrees with experiment in the ratio of the peak to other energies.

4. Experimental results show quadrupole magnet is not efficient in collecting positrons, since positrons have large angular distribution. Solenoid can be used to improve the collection efficiency of positrons [20] and should be placed as close the production target as possible for better efficiency.

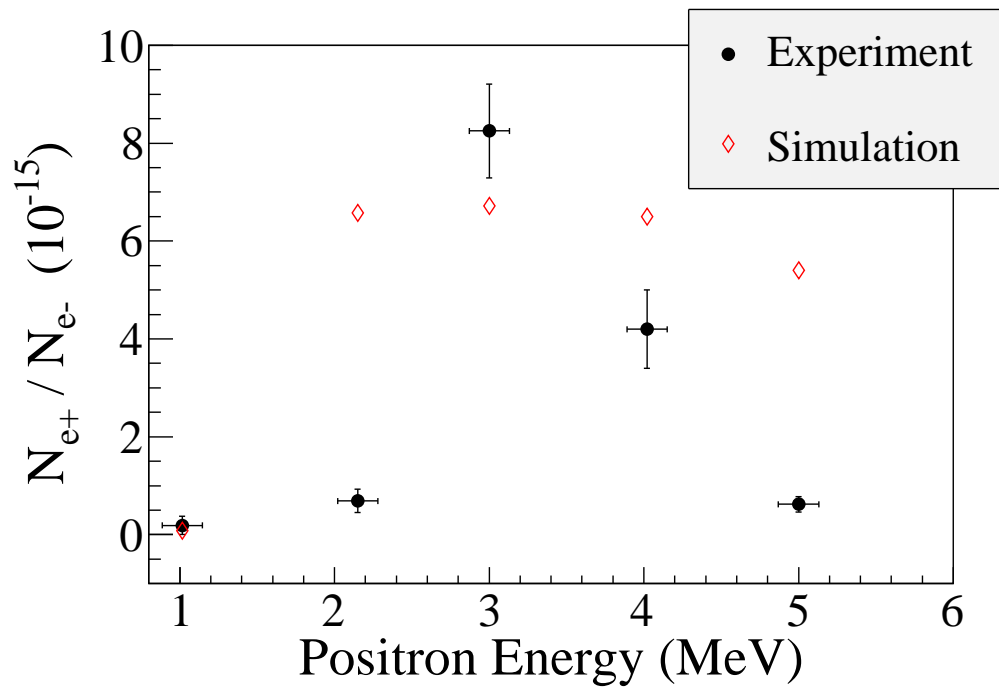


Figure 5.1: Ratio of positrons detected to electrons in experiment and simulation.

Appendix A

Electron Beam Energy Scan

Electron beam energy was scanned using dipole magnet. The dipole magnet was set to bend electron beam with certain energy. The beam current corresponding to that bent electron beam energy was observed on a Faraday cup and oscilloscope.

Table A.1: Dipole Magnet Mapping Data.

Dipole Magnet Coil Current (A)	Faraday Cup Current (mA)	Electron Beam Energy (MeV)
8	0.5	4.3119
9	0.6	4.8896
10	0.67	5.4570
11	0.716	6.0141
12	0.752	6.5610
13	0.828	7.0975
14	0.896	7.6238
15	1.112	8.1399
16	1.328	8.6456
17	1.624	9.1411
18	1.896	9.6262
19	2.448	10.1012
20	3.36	10.5658

Continued on next page

Table A.1 – *Continued from previous page*

Dipole Magnet Coil Current (A)	Faraday Cup Current (mA)	Electron Beam Energy (MeV)
21	4.82	11.0201
22	6.58	11.4642
22.2	7.88	11.5518
22.5	9.24	11.6824
22.7	10.0	11.7690
23	10.2	11.8980
23.1	11.2	11.9408
23.2	11.56	11.9836
23.3	13.04	12.0262
23.5	13.2	12.1111
23.8	13.04	12.2377
24	13.48	12.3216
24.2	12.36	12.4050
24.5	11.24	12.5295
24.7	10.2	12.6119
25	10.28	12.7348
25.1	8.6	12.7756
25.2	6.92	12.8162
25.5	6.2	12.9376
25.7	4.84	13.0180
26	3.64	13.1378
26.5	1.82	13.3354
27	1.28	13.5305

Continued on next page

Table A.1 – *Continued from previous page*

Dipole Magnet Coil Current (A)	Faraday Cup Current (mA)	Electron Beam Energy (MeV)
28	0.56	13.9129
29	0.364	14.2850
30	0.364	14.6469

Appendix B

Electron Beam Energy Scan

B.1 Emittance Calculator

```
% Emit_Calc.m
% Reads images from files and digitize images.
% Fits a super Gaussian function on the projection, get the rms values.
% Then pass them to fit parabola
%
% April-2011
% Sadiq Setiniyaz

clc;
clear

me = 0.511; % electron rest mass in MeV
%En = 14; %enter beam energy here in MeV unit.
En = 14.9985 ; %14.9985 MeV energy at Mar 17th, 2011.
En_er = En*0.1; % Assume 5% error on Energy
L = 0.08; % pole face is 8 cm long in z direction.
R_Bore = 0.0254; %Radius of the Bore aperture = center to pole face = 1 inch.
%L_ef = L + R_Bore;
%I_max_neg = -10; %enter smallest negative scan current. Here -7 Amps
```



```

%I_max_pos = 7; %enter biggest positive scan current. Here 10 Amps
I_start=-3.0; % Scan starting current
%I_end=-2.0; % Scan ending current
I_increment=0.2;
scan_current_number=31; % do 13 scan.
scan_times=7;

%for ii = 1:scan_step
%    I(ii) = I_start + (ii-1)*I_increment;
%end

p = sqrt(En*En - me*me)/1000;% e- momentum in GeV/c

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% Enter the distance from the center of the quad to the screen
S12=3.1;%(in m unit) S12(q4)=1.875 cm. S12(q1)=3.10 cm
erS12 = 0.005; % assume 51 mm error.
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%Enter calibration here:
calibration_x=0.04327*0.001; %m/px
calibration_y=0.04204*0.001; %m/px
er_calibration_x=0.00016*0.001;
er_calibration_y=0.00018*0.001;
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

disp('Reading image ...')

```

```
% Get image for background. For background RF is on, gun is off.
```

```
bg1 = imread('Scan_1\RF_on_Gun_off_bg.bmp');  
bg2 = imread('Scan_2\RF_on_Gun_off_bg.bmp');  
bg3 = imread('Scan_3\RF_on_Gun_off_bg.bmp');  
bg4 = imread('Scan_4\RF_on_Gun_off_bg.bmp');  
bg5 = imread('Scan_5\RF_on_Gun_off_bg.bmp');  
bg6 = imread('Scan_6\RF_on_Gun_off_bg.bmp');  
bg7 = imread('Scan_7\RF_on_Gun_off_bg.bmp');  
% Averaging background.  
bg = (bg1+bg2+bg3+bg4+bg5+bg6+bg7+bg7+bg7)/7;  
imd_bg = double(bg(:,:,1));
```

```
for ii=1:scan_times
```

```
switch ii
```

```
case 1
```

```
    addpath(genpath('\Scan_1'));
```

```
case 2
```

```
    addpath(genpath('\Scan_2'));
```

```
case 3
```

```
    addpath(genpath('\Scan_3'));
```

```
case 4
```

```
    addpath(genpath('\Scan_4'));
```

```
case 5
```

```
    addpath(genpath('\Scan_5'));
```

```
case 6
```

```
    addpath(genpath('\Scan_6'));
```

```
case 7
```

```

        addpath(genpath('\Scan_7'));
end

% Read OTR images.
for scan = 1:scan_current_number;
    thisfilename=ii;
    imNo = ii;
    I(scan) = I_start + (scan-1)*I_increment;
    switch scan
        case 1
            % Devide the effetive length by 100 to convert to meter unit.
            im = imread('negative\11.bmp');
            tifname='11';
            L_ef(scan) = 9.95/100;
            Er_L_ef(scan) = 0.17/100;
        case 2
            im = imread('negative\12.bmp'); % reading 1.png
            tifname='12';
            L_ef(scan) = 9.91/100;
            Er_L_ef(scan) = 0.16/100;
        case 3
            im = imread('negative\13.bmp');
            tifname='13';
            L_ef(scan) = 9.91/100;
            Er_L_ef(scan) = 0.16/100;
        case 4
            im = imread('negative\14.bmp');
            tifname='14';

```

```
L_ef(scan) = 9.85/100;
Er_L_ef(scan) = 0.14/100;
case 5
    im = imread('negative\15.bmp');
    tifname='15';
    L_ef(scan) = 9.85/100;
    Er_L_ef(scan) = 0.16/100;
case 6
    im = imread('negative\16.bmp');
    tifname='16';
    L_ef(scan) = 9.87/100;
    Er_L_ef(scan) = 0.19/100;
case 7
    im = imread('negative\17.bmp');
    tifname='17';
    L_ef(scan) = 9.82/100;
    Er_L_ef(scan) = 0.19/100;
case 8
    im = imread('negative\18.bmp');
    tifname='18';
    L_ef(scan) = 9.86/100;
    Er_L_ef(scan) = 0.17/100;
case 9
    im = imread('negative\19.bmp');
    tifname='19';
    L_ef(scan) = 9.73/100;
    Er_L_ef(scan) = 0.18/100;
case 10
```

```

    im = imread('negative\20.bmp');
    tiffname='20';
    L_ef(scan) = 9.65/100;
    Er_L_ef(scan) = 0.22/100;
case 11
    im = imread('negative\21.bmp');
    tiffname='21';
    L_ef(scan) = 9.71/100;
    Er_L_ef(scan) = 0.22/100;
case 12
    im = imread('negative\22.bmp');
    tiffname='22';
    L_ef(scan) = 9.58/100;
    Er_L_ef(scan) = 0.23/100;
case 13
    im = imread('negative\23.bmp'); % reading 1.png
    tiffname='23';
    L_ef(scan) = 9.45/100;
    Er_L_ef(scan) = 0.25/100;
case 14
    im = imread('negative\24.bmp');
    tiffname='24';
    L_ef(scan) = 9.16/100;
    Er_L_ef(scan) = 0.27/100;
case 15
    im = imread('negative\25.bmp');
    tiffname='25';
    L_ef(scan) = 8.80/100;

```

```
Er_L_ef(scan) = 0.26/100;
case 16
im = imread('negative\26.bmp');
tifname='26';
L_ef(scan) = 8.26/100;
Er_L_ef(scan) = 0.38/100;
case 17
im = imread('positive\27.bmp');
tifname='27';
L_ef(scan) = 8.88/100;
Er_L_ef(scan) = 0.25/100;
case 18
im = imread('positive\28.bmp');
tifname='28';
L_ef(scan) = 9.12/100;
Er_L_ef(scan) = 0.22/100;
case 19
im = imread('positive\29.bmp');
tifname='29';
L_ef(scan) = 9.28/100;
Er_L_ef(scan) = 0.19/100;
case 20
im = imread('positive\30.bmp');
tifname='30';
L_ef(scan) = 9.47/100;
Er_L_ef(scan) = 0.27/100;
case 21
im = imread('positive\31.bmp');
```

```
tifname='31';
L_ef(scan) = 9.55/100;
Er_L_ef(scan) = 0.20/100;

case 22
    im = imread('positive\32.bmp');
    tifname='32';
    L_ef(scan) = 9.66/100;
    Er_L_ef(scan) = 0.29/100;

case 23
    im = imread('positive\33.bmp');
    tifname='33';
    L_ef(scan) = 9.73/100;
    Er_L_ef(scan) = 0.22/100;

case 24
    im = imread('positive\34.bmp');
    tifname='34';
    L_ef(scan) = 9.80/100;
    Er_L_ef(scan) = 0.18/100;

case 25
    im = imread('positive\35.bmp');
    tifname='35';
    L_ef(scan) = 9.72/100;
    Er_L_ef(scan) = 0.17/100;

case 26
    im = imread('positive\36.bmp');
    tifname='36';
    L_ef(scan) = 9.81/100;
```

```

        Er_L_ef(scan) = 0.12/100;
case 27
    im = imread('positive\37.bmp');
    tifname='37';
    L_ef(scan) = 9.84/100;
    Er_L_ef(scan) = 0.10/100;
case 28
    im = imread('positive\38.bmp');
    tifname='38';
    L_ef(scan) = 9.90/100;
    Er_L_ef(scan) = 0.11/100;
case 29
    im = imread('positive\39.bmp');
    tifname='39';
    L_ef(scan) = 9.91/100;
    Er_L_ef(scan) = 0.12/100;
case 30
    im = imread('positive\40.bmp');
    tifname='40';
    L_ef(scan) = 9.92/100;
    Er_L_ef(scan) = 0.16/100;
case 31
    im = imread('positive\41.bmp');
    tifname='41';
    L_ef(scan) = 9.94/100;
    Er_L_ef(scan) = 0.18/100;
end
sg = im; % reading 1.png

```



```

imd_sg = double(sg(:,:,1));
pic = (imd_sg-imd_bg);
%imd = imd_sg;
%imd = imd_bg;

% Noise Cleaning.
% Getting rid of the dead pixels.
% If there is sudden increase in the pixel brightness,
% Then use the pixel brightness of the earlier pixel.
for i = 3:768
for j = 3:576
    if pic(j,i)>500
        pic(j,i)=pic(j-1,i);
    elseif pic(j,i)-pic(j-2,i)>20
        pic(j,i)=pic(j-1,i);
    end
end
end

% Determine image size in pixels.
dim=size(pic);
%dim=size(imd);
dim_x = dim(1);
dim_y = dim(2);

xunit='m';
yunit='m';

```

```

% Beam transverse profiles.
profx = sum(pic,1); % make x projection
profy = sum(pic,2)'; % make y projection

xbins=size(profx);
ybins=size(profy);
x=(1:1:xbins(2));
y=(1:1:ybins(2));

% Set Gaussian fit range.
xl = 1;
xr = 766;
yl = 1;
yr = 576;

% Checking.
%plot(x,profx,'k');
%hold on;
%plot(y,profy,'k');
%hold on;

% Initialize fit parameters.
% a1= base. a2 = A; amplitude. a3 = mean. a4 = D; sigma_0. a5 = N;
a1 = 100;
a2 = 7700;
a3 = 280;
a4 = 39;

```

```

a5 = 1;

% SupGau = a(1)+a(2)*exp(-abs(X-a(3))/(a(4))).^a(5); % super gaussian.
% Putting the parameters together.
a0 = [a1,a2,a3,a4,a5];
% Setting fit criteria and use fminsearch optimization.
opts = optimset('TolX',1e-4,'MaxFunEvals',10000,'MaxIter',10000,'Display','on');
% Pass fit parameters to SupGau_devsum.
[fitpara_x,fval_x,flag_x,err_x] = fminsearch(@SupGau_devsum,a0,opts,x,prof_x);
[fitpara_y,fval_y,flag_y,err_y] = fminsearch(@SupGau_devsum,a0,opts,y,prof_y);
% Get the fit parameters of x profile.
base_x = fitpara_x(1);
amplitude_x = fitpara_x(2);
peak_center_x = fitpara_x(3);
sig0_x = fitpara_x(4);
N_x = fitpara_x(5);
sig_x(scan,imNo) = sig0_x*(pi/2).^(2/fitpara_x(5)-1);
% Get the fit parameters of y profile
base_y = fitpara_y(1);
amplitude_y = fitpara_y(2);
peak_center_y = fitpara_y(3);
sig0_y = fitpara_y(4);
N_y = fitpara_y(5);
sig_y(scan,imNo) = sig0_y*(pi/2).^(2/fitpara_y(5)-1);

% Printing out parameters to check.
string_x = [
    num2str(I(scan),' %2.2f'), ' ', ...

```

```

    num2str(imNo,'%d'),' ', ...
    num2str(base_x,'%12.2f'),' ', ...
    num2str(amplitude_x,'%12.f'),' ', ...
    num2str(peak_center_x,'%12.2f'),' ', ...
    num2str(N_x,'%12.4f'),' ', ...
    num2str(sig0_x,'%12.2f'),' ', ...
    num2str(sig_x(scan,imNo),'%12.2f'),' ', ...
];
%disp(string_x);
string_y = [
    num2str(I(scan),' %2.2f'),' ', ...
    num2str(imNo,'%d'),' ', ...
    num2str(base_y,'%12.2f'),' ', ...
    num2str(amplitude_y,'%12.f'),' ', ...
    num2str(peak_center_y,'%12.2f'),' ', ...
    num2str(N_y,'%12.4f'),' ', ...
    num2str(sig0_y,'%12.2f'),' ', ...
    num2str(sig_y(scan,imNo),'%12.2f'),' ', ...
];
%disp(string_y);
%sig

% Plot to check.
%plot(x,profx,'k');
%hold on;
%plot(y,profy,'k');
%hold on;

```

```

% Construct fit curve from the fit parameters.
y_fit_x = fitpara_x(1)+fitpara_x(2)*exp( -0.5*(abs(x-fitpara_x(3))/
(fitpara_x(4))).^fitpara_x(5) );
y_fit_y = fitpara_y(1)+fitpara_y(2)*exp( -0.5*(abs(y-fitpara_y(3))/
(fitpara_y(4))).^fitpara_y(5) );

%plot(x,y_fit_x,'r');

%plot(y,y_fit_y,'r');
drawnow
end
end

for scan=1:scan_current_number

% Find mean and standar deviation.
sig_mean_x(scan) = mean(sig_x(scan,:));
sig_mean_y(scan) = mean(sig_y(scan,:));
sig_x_er(scan)   = std(sig_x(scan,:));
sig_y_er(scan)   = std(sig_y(scan,:));

% Converting from pixels to length (in m unit).
sig_mean_x(scan)=sig_mean_x(scan)*calibration_x; %
sig_mean_y(scan)=sig_mean_y(scan)*calibration_y; %
sig_x_er(scan)= sqrt((sig_x_er(scan)*calibration_x).^2+(sig_mean_x(scan)*
er_calibration_x).^2);
sig_y_er(scan)= sqrt((sig_y_er(scan)*calibration_y).^2+(sig_mean_y(scan)*

```

```

er_calibration_y).^2);

% Squared sigma.
sig_sqr_x(scan) = sig_mean_x(scan)*sig_mean_x(scan);
sig_sqr_x_er(scan) = 2*sig_mean_x(scan)*sig_x_er(scan);
sig_sqr_y(scan) = sig_mean_y(scan)*sig_mean_y(scan);
sig_sqr_y_er(scan) = 2*sig_mean_y(scan)*sig_y_er(scan);

%I(scan) = I_start + (scan-1)*I_increment;
%plot(I,sig_mean,'r');
%Get the quarupole strength and its error from the dipole current.
k1(scan) =0.2998*(3.6*0.0001+1945*0.000001*I(scan))/(0.0254*p);

k1_Er(1) =0.2998*((3.6+1.3)*0.0001+(1945+2)*0.000001*I(scan))/(0.0254*p);
k1_Er(2) =0.2998*((3.6-1.3)*0.0001+(1945+2)*0.000001*I(scan))/(0.0254*p);
k1_Er(3) =0.2998*((3.6+1.3)*0.0001+(1945-2)*0.000001*I(scan))/(0.0254*p);
k1_Er(4) =0.2998*((3.6-1.3)*0.0001+(1945-2)*0.000001*I(scan))/(0.0254*p);
er_k1(1)=abs(k1(scan)-k1_Er(1));
er_k1(2)=abs(k1(scan)-k1_Er(2));
er_k1(3)=abs(k1(scan)-k1_Er(3));
er_k1(4)=abs(k1(scan)-k1_Er(4));

k1_er(scan)=max(er_k1);

k1L(scan) = L_ef(scan)*k1(scan); %k1*L
er_k1L(scan) = sqrt((L_ef(scan)*k1_er(scan) )^2+(Er_L_ef(scan)*k1(scan))^2);
%er_k1L(scan) = L_ef*k1_er(scan);

```

```

% Put the parameters together to pass to parabolic fits
FitDatX = [k1L',er_k1L',sig_sqr_x',sig_sqr_x_er'];
FitDatY = [k1L',er_k1L',sig_sqr_y',sig_sqr_y_er'];

end

X_fit_data = fopen('X_fit_data.txt','w');
Y_fit_data = fopen('Y_fit_data.txt','w');
fprintf(X_fit_data,'%4f %4f %4f %4f \n',k1L(16:31)',er_k1L(16:31)',
sig_sqr_x(16:31)*10^6',sig_sqr_x_er(16:31)*10^6');
fprintf(Y_fit_data,'%4f %4f %4f %4f \n',k1L(2:15)',er_k1L(2:15)',
sig_sqr_y(2:15)*10^6', sig_sqr_y_er(2:15)*10^6');
fprintf(X_fit_data,'%4f %4f %4f \n',k1L(16:31)', sig_sqr_x(16:31)''*10^6,
sig_sqr_x_er(16:31)''*10^6);
fprintf(Y_fit_data,'%4f %4f %4f \n',k1L(2:15)', sig_sqr_y(2:15)''*10^6,
sig_sqr_y_er(2:15)''*10^6);
fclose(X_fit_data);
fclose(Y_fit_data);

% Converting to cgs (mm and mrad) units.
[k1L(16:31)' sig_sqr_x(16:31)''*10^6 sig_sqr_x_er(16:31)''*10^6]
[k1L(2:15)' sig_sqr_y(2:15)''*10^6 sig_sqr_y_er(2:15)''*10^6]

%Emit_Parabola_Fit_kl_XProjection(k1L,er_k1L,sig_sqr_x,sig_sqr_x_er,me,En,
S12,erS12,scan_current_number);
%Emit_Parabola_Fit_kl_YProjection(k1L,er_k1L,sig_sqr_y,sig_sqr_y_er,me,En,
S12,erS12,scan_current_number);

```

```
Emit_Parabola_Fit_kl_XProjection(k1L(16:31),er_k1L(16:31),
sig_sqr_x(16:31)*10^6,sig_sqr_x_er(16:31)*10^6,me,En,En_er,S12,erS12,16);
Emit_Parabola_Fit_kl_YProjection(k1L(2:15) ,er_k1L(2:15),
sig_sqr_y(2:15)*10^6, sig_sqr_y_er(2:15)*10^6, me,En,En_er,S12,erS12,14);
```

B.2 Super Gaussian Fit

This function is being called during by EmitCalc.m to fit super Gaussian to beam transverse profile.

```
function chisq = SupGau_devsum(a,X,Y)
% a(1) = base
% a(2) = A; %amplitude
% a(3) = x0; %center
% a(4) = D; %sigma_0
% a(5) = N; %N=2 is normal Gaussian.
           %N<super Gaussian (sharp top).
           %N>Flat top shape Gaussian.
SupGau = a(1)+a(2)*exp( -0.5*(abs(X-a(3))/(a(4))).^a(5) ); % super Gaussian
csq = (Y - SupGau).^2;
chisq = sum(csq);
return
```

B.3 Parabolic Fit

This function will fit parabola for given rms values, plot them and from parabola parameters extract emittance.

```
function varargout = Emit_Parabola_Fit_kl_XProjection(x,erx,y,ery,me,En,
```



```

En_er,S12,erS12,NumPoints)

%x
%y
%ery

order = 2; % second order fit
ParNum = order + 1;

% finding row matrix beta
for k=1:ParNum
for i=1:NumPoints
    f(k)=power(x(i),k-1);
    %fprintf(' i=%d f(%d)=%g \t',i,k,f(k));
    beta_element(k,i)=y(i)*f(k)/(ery(i)*ery(i));
    %fprintf('y(i=%d)=%g ery(i=%d)=%g \n',i,y(i),i,ery(i));
    %fprintf('beta(k=%d,i=%d)=%g \n',k,i,beta_element(k,i));
    beta(k)=sum(beta_element(k,:));
    %fprintf('beta_element(%d,%d)=%g
    %beta(%d)=%g\n',k,i,beta_element(k,i),k,beta(k));
end
end
%beta

% finding matrix alpha
for k=1:ParNum
for l=1:ParNum
    for i=1:NumPoints

```

```

    f(k)=power(x(i),k-1);
    f(l)=power(x(i),l-1);
    alpha_element(k,l,i)=f(k)*f(l)/(ery(i)*ery(i));
    alpha(k,l)=sum(alpha_element(k,l,:));
    %fprintf('alpha_element(%d,%d,%d)=%g alpha(%d,%d)=%g\n',k,l,i,
    alpha_element(k,l,i),k,l,alpha(k,l));
end
end
end
%alpha

%To find fit parameters, need to invert matrix alpha.
alpha_invert = inv(alpha);
%alpha_invert

% The fit is  $y = a(1) + a(2)*x + a(3)*x*x$ 
%fit parameters by matrix inversion method
parameter = beta*alpha_invert; %a(1)=parameter(1)
%parameters
fit_m_inver = parameter(1) + parameter(2)*x + parameter(3)*x.*x;
% error on the parameters
er_a = sqrt(diag(alpha_invert));

%fit parameters by MatLab
par = polyfit(x,y,2);
%par
fit_MatLab = par(3) + par(2)*x + par(1)*x.*x;

```

```

%Get Emittance and Twiss parameters from fit
gamma = En/me;
er_gamma = En_er/me;
beta = sqrt(1-1/gamma^2);
er_beta = er_gamma/(gamma^3*beta);

A=parameter(3);
B=-parameter(2)/(2*A);
C=parameter(1)-A*B^2;
erA = er_a(3);
erB = sqrt( (-er_a(2)/(2*A))^2 + (parameter(2)*erA/(2*A^2))^2 );
erC = sqrt((er_a(1))^2 + (-B^2*erA)^2 + (-2*A*B*erB)^2);
fprintf('A=%g+-%g B=%g+-%g C=%g+-%g\n',A,erA,B,erB,C,erC);

emit = sqrt(A*C)/((S12)^2);
er_emit = sqrt( (1/2*A^(-1/2)*A^(1/2)*erA/(S12)^2)^2 +
(1/2*A^(1/2)*A^(-1/2)*erC/(S12)^2)^2 + ( 2*sqrt(A*C)*erS12/(S12)^3)^2 );
emit_n = emit*gamma;
er_emit_n = sqrt((emit*er_gamma*beta)^2+(emit*gamma*er_beta)^2+
(er_emit*gamma*beta)^2);
beta_func = sqrt(A/C);
er_beta_func = sqrt( (1/2*sqrt(1/(A*C))*erA)^2 + (-1/2*sqrt(A/C^3)*erC)^2 );
alpha_func = beta_func*(B + 1/S12);%alpha_func = sqrt(A/C)*(B + 1/S12)
er_alpha_func = sqrt(((B+1/S12)*er_beta_func)^2 + (beta_func*erB)^2 +
(-beta_func*erS12/(S12)^2)^2 );

figure(1)

```

```

set(axes,'FontSize',40)
pardat = errorbar(x,y,ery,'MarkerSize',30,'Marker','.', 'LineStyle','none',...
'LineWidth',3,...
'DisplayName','Data Points',...
'Color',[0 0 1]);
hold on

%Plot fit done by matrix inversion method.
parfit_m_inver = plot(x,fit_m_inver,'r');
set(parfit_m_inver,'LineWidth',3);

legend('Data','Fit');
set(legend,'Position',[0.73 0.75 0.1 0.1]);
set(legend,'FontSize',40);
set(legend,'FontName','Times New Roman');

hx = xlabel('k_{1}L (m^{-1})','FontSize',48,'FontName','Times New Roman');
hy = ylabel('\sigma^2_x (mm^2)','FontSize',48,'FontName','Times New Roman');
box off; % remove the top and right axes

%set(gca,'ticklength',4*get(gca,'ticklength'));
set(gca,'ticklength',[0.06 0.9]);
fit=title('');
%fit=title('15.6 MeV, X-Projection: k_{1}L vs \sigma^2');
set(fit,'FontSize',24,'FontWeight','bold','FontName','Times New Roman');
axis([-0.05 0.55 2.3 3.2]); %axis([xmin xmax ymin ymax])
%axis('FontSize',28);

```

```

saveas(fit,'Emit_Calc_plots\par_fit_x.fig','fig');
saveas(fit,'Emit_Calc_plots\par_fit_x.eps','epsc');
saveas(fit,'C:\Users\sadiq\Desktop\IPAC12\Paper\par_fit_x.eps','epsc');
saveas(fit,'Emit_Calc_plots\par_fit_x.png','png');
drawnow

fprintf('x-projection:\n\nemit=%.3f +- %.3f mm*mrاد, emit_norm=%.2f +-
%.2f mm*mrاد \n\n', emit, er_emit, emit_n, er_emit_n);
fprintf('beta=%.2f +- %.2f m, alpha=%.2f +- %.2f rad \n\n', beta_func,
er_beta_func, alpha_func, er_alpha_func);
fprintf('parabola fit for y-projection (y in mm unit): \n y = (%.5f +-.5f)
+ (%.5f+-.5f)*x + (%.5f+-.5f)*x.*x \n\n', parameter(1),er_a(1),
parameter(2),er_a(2), parameter(3),er_a(3));
return

```

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