Measurement of the $x$- and $Q^2$-Dependence of the Asymmetry $A_1$ on the Nucleon


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We report results for the virtual photon asymmetry $A_1$ on the nucleon from new Jefferson Lab measurements. The experiment, which used the CEBAF Large Acceptance Spectrometer and longitudinally polarized proton ($^{15}$NH$_4$) and deuteron ($^{15}$ND$_3$) targets, collected data with a longitudinally polarized electron beam at energies between 1.6 GeV and 5.7 GeV. In the present paper, we concentrate on our results for $A_1(x, Q^2)$ and the related ratio $g_1/F_1(x, Q^2)$ in the resonance and the deep inelastic regions for our lowest and highest beam energies, covering a range in momentum transfer $Q^2$ from 0.05 to 5.0 GeV$^2$ and in final-state invariant mass $W$ up to about 3 GeV. Our data show detailed structure in the resonance region, which leads to a strong $Q^2$-dependence of $A_1(x, Q^2)$ for $W$ below 2 GeV. At higher $W$, a smooth approach to the scaling limit, established by earlier experiments, can be seen, but $A_1(x, Q^2)$ is not strictly $Q^2$-independent. We add significantly to the world data set at high $x$, up to $x = 0.6$. Our data exceed the SU(6)-symmetric quark model expectation for both the proton and the deuteron while being consistent with a negative $d$-quark polarization up to our highest $x$. This data set should improve next-to-leading order (NLO) pQCD fits of the parton polarization distributions.

PACS numbers: 13.60.Hb, 13.88.+e, 14.20.Dh
Keywords: Spin structure functions, nucleon structure

The spin structure of the nucleon has been investigated in a series of much-discussed polarized lepton scattering experiments over the last 25 years. These measurements, most of which covered the deep inelastic scattering (DIS) region of large final-state invariant mass $W$ and momentum transfer $Q^2$, compared the $Q^2$-dependence of the polarized structure function $g_1$ with QCD expectations and shed new light on the structure of the nucleon. Among the most surprising results was the realization that only a small fraction of the nucleon spin (20% - 30%) is carried by the quark helicities, in disagreement with quark model expectations of 60% - 75%. This reduction is often attributed to the effect of a negatively polarized quark sea at low momentum fraction $x$, which is typically not included in quark models (see the paper by Isgur for a detailed discussion).

For a more complete understanding of the quark structure of the nucleon, it is advantageous to concentrate on a kinematic region where the scattering is most likely to occur from a valence quark in the nucleon carrying more than a fraction $x = 1/3$ of the nucleon momentum. In particular, the virtual photon asymmetry, $A_1(x) \approx g_1(x)/F_1(x)$, (where $F_1$ is the usual unpolarized structure function) can be (approximately) interpreted in terms of the polarization $\Delta u/u$ and $\Delta d/d$ of the valence $u$ and $d$ quarks in the proton in this kinematic region, where the contribution from sea quarks is minimized. This asymmetry also has the advantage of showing smaller scaling violations than the structure functions $g_1$ and $F_1$ individually, making a comparison with various theoretical models and predictions more straightforward.

By measuring $A_1(x)$ at large $x$, one can test different predictions about the limit of $A_1(x)$ as $x \rightarrow 1$. Nonrelativistic Constituent Quark Models (CQM) based on SU(6) symmetry predict $A_1(x) = 5/9$ for the proton, $A_1(x) = 0$ for the neutron and $A_1(x) = 1/3$ for the deuteron (modified by a factor $(1 - 1.5 w_D)$ for the D-state probability $w_D$ in the deuteron wave function). Quark
models that include some mechanism of SU(6) symmetry breaking (e.g., one-gluon exchange hyperfine interaction between quarks \cite{14}) predict that \( A_1(x) \to 1 \) for all three targets as \( x \to 1 \). This is because target remnants with total spin 1 are suppressed relative to those with spin 0. The same limit for \( x \to 1 \) is also predicted by pQCD \cite{15}, because hadron helicity conservation suppresses the contribution from quarks anti-aligned with the nucleon spin. In this case, \( A_1(x) \) would be predicted to be more positive at moderately large \( x < 1 \) because both \( u \) and \( d \) quarks contribute with positive polarization \cite{16}. Finally, a recent paper \cite{17} connected the behavior of \( A_1(x) \) at large \( x \) with the dynamics of resonance production via duality, leading to several predictions for the approach to \( A_1(x \to 1) = 1 \) that depend on the mechanism of SU(6) symmetry breaking.

Clearly, measurements of the asymmetry \( A_1 \) at moderate to high \( x \geq 0.3 \) are an indispensable tool to improve our understanding of the valence structure of the nucleon. Although many data already exist on \( A_1(x, Q^2) \), most of the high-energy data have very limited statistics at large \( x \) and therefore large uncertainties. High-precision data so far exist only for a \(^3\)He target \cite{18} (which can be used to approximate \( A_1 \) for a free neutron). Those data show for the first time a positive asymmetry \( A_1 \) at large \( x \), but agree better with predictions \cite{14} that assume negative \( d \)-quark polarization \( \Delta d/d \) even at large \( x \).

In this paper, we report the first high-precision measurement of \( A_1(x, Q^2) \) for the proton and the deuteron at moderate to large \( x (x \geq 0.15) \) over a range of momentum transfers \( Q^2 = 0.05 \cdots 5.0 \) GeV\(^2\), covering both the resonance and the deep inelastic region.

The data described in this paper were collected during the second polarized target run (2000–2001) with CLAS in Hall B of the Thomas Jefferson National Accelerator Facility (TJNAF – Jefferson Lab). Results from the first run with beam energies of 4.2 and 2.5 GeV were recently published \cite{12, 13}. The present data extend the kinematic coverage significantly to both lower and higher values of \( Q^2 \) (covering nearly two orders of magnitude, instead of only one), and to higher values of \( W \), covering much more of the DIS region (nearly doubling the range in \( x \)). Longitudinally polarized electrons of several beam energies around 1.6 GeV and 5.7 GeV were scattered off longitudinally polarized ammonia targets — \(^{15}\)NH\(_3\) and \(^{15}\)ND\(_3\) — and detected in the CEBAF Large Acceptance Spectrometer (CLAS). A detailed description of CLAS may be found in Ref. \cite{18}. The spectrometer is equipped with a superconducting toroidal magnet and three drift chamber regions that cover up to 80% of the azimuthal angles and reconstruct the momentum of charged particles scattering within a polar angular range between 8° and 142°. (Due to obstruction by the polarized target Helmholtz coils only scattering angles up to 50° were accessible during our experiment.) We used both the inbending (for electrons) and the outbending torus magnetic field orientations, to extend the coverage in \( Q^2 \).

An array of scintillator counters covers the above angular range and is used to determine the time of flight for charged particles. A forward angle electromagnetic calorimeter 16 radiation lengths thick covers polar angles up to 45° and is used along with the drift chambers to separate pions from electrons for this analysis. A gas Cherenkov detector covering the same angular range as the calorimeter is used in conjunction with the calorimeter to create a coincidence trigger, and to reject pions.

The target material was kept in a 1 K liquid Helium bath and was polarized via Dynamic Nuclear Polarization (DNP) \cite{19}. The target polarization was monitored online using a Nuclear Magnetic Resonance (NMR) system. The beam polarization was measured at regular intervals with a Moller polarimeter. The product of beam and target polarization \( P_bP_t \) was determined from the well-known asymmetry for elastic (quasielastic) scattering from polarized protons (deuterons), measured simultaneously with inelastic scattering. For the 1.6 GeV data set, the average polarization product was \( P_bP_t = 0.54 \pm 0.005 \) (0.18 \pm 0.007) for the \(^{15}\)NH\(_3\) \((^{15}\)ND\(_3\)) target. The corresponding value for the 5.7 GeV data set was \( 0.51 \pm 0.01 \) (0.19 \pm 0.03).

The data analysis proceeds along the following steps (see Ref. \cite{13} for details). We first extract the raw count asymmetry \( A_{1\text{raw}} = (N^+ - N^-)/(N^+ + N^-) \), where the electron count rates for anti-parallel \( (N^+) \) and parallel \( (N^-) \) electron and target polarization are normalized to the (live-time gated) beam charge for each helicity. The background due to misidentified pions and electrons from decays into \( e^+e^- \) pairs has been subtracted from these rates. We divide the result by the product of beam and target polarization \( P_bP_t \) and correct for the contribution from non-hydrogen nuclei in the target. For this purpose, we use auxiliary measurements on \(^{12}\)C, \(^{4}\)He and \(^{15}\)N targets. We then combine the asymmetries for different beam and target polarization directions, thereby reducing any systematic errors from false asymmetries (no significant differences between the different polarization sets were found). Finally we apply radiative corrections using the code RCSLACPOL \cite{20} which follows the prescription by Kuchto and Shumeiko \cite{20} for the internal corrections and by Tsai \cite{21} for the external corrections. The (quasi-)elastic radiative tail contribution to the denominator of the asymmetry is treated as a further dilution factor \( f_{RC} \).

The final result is the longitudinal (Born) asymmetry \( A_1 = D(A_1 + \eta A_2) \), where the depolarization factor \( D = (1 − E'\epsilon/E)/(1 + R) \), \( E'(\epsilon) \) is the beam (scattered electron) energy, \( \epsilon = (2EE' − Q^2/2)/(E' + E^2 + Q^2/2) \) is the virtual photon polarization, \( R \approx 0.2 \) is the ratio of the longitudinal to the transverse photoabsorption cross section and \( \eta = (\epsilon \sqrt{Q^2})/(E − E'\epsilon) \). \( A_2 \) is the longitudinal-transverse interference virtual photon
asymmetry. We use the standard notations for the energy transfer, \( \nu = E - E' \), and four-momentum transfer squared, \( Q^2 = 4EE'\sin^2(\theta/2) \).

Finally, using a parametrization of the world data to model \( A_2 \) and \( R \), we extract \( A_1 \) and the closely related ratio \( g_1/F_1 \):

\[
\frac{g_1}{F_1}(x, Q^2) = \frac{1}{(\gamma^2 + 1)} \left( \frac{A_{||}}{D} + (\gamma - \eta)A_2 \right) \tag{1}
\]

with \( \gamma^2 = Q^2/\nu^2 \). The extraction of this ratio is typically less dependent on the unmeasured asymmetry, \( A_2 \), than that of the asymmetry \( A_1 \). Our parametrization includes input from phenomenological models AO and MAID as well as fits to the polarized data from the first run with CLAS and to unpolarized structure functions measured in Jefferson Lab’s Hall C. More details of the parametrization and the data analysis can be found in Ref. [13]. Since \( A_1 \) and \( g_1/F_1 \) are independent of beam energy for given \((x, Q^2)\) values, we combine (after consistency checks) our results for each bin in \((x, Q^2)\) for all beam energies and CLAS torus magnetic field settings.

To estimate systematic uncertainties on our final results, we vary all input parameters and models within realistic limits and study the induced variations of the asymmetry \( A_1 \). We then add all these variations in quadrature to get the total systematic uncertainty. Among the sources of systematic errors we considered are uncertainties on the product of beam and target polarization and various inputs in our determination of the dilution factor (target dimensions, nuclear cross sections, and contributions from polarized nuclei other than the hydrogen isotope under consideration). We also estimate the remaining contribution from misidentified pions and electrons from pair-symmetric decay processes. Finally, we varied all model parametrizations for unpolarized \((F_1, R)\) and polarized \((A_1, A_2)\) structure functions used both in the extraction of \(A_1\) and \(g_1/F_1\) and in our radiative corrections. Systematic errors are indicated by shaded bands in the figures.

A small sample of our results on the asymmetry \( A_{||}/D \) for the proton is shown in Fig. 1. Since the asymmetry \( A_2 \) contributes only very little to these data (see dashed line in the figure), they are essentially equal to \( A_1 \). A strong dependence of this asymmetry on the final state mass \( W \) can be seen, especially at low \( Q^2 \) (top left panel). Our total data set covers 19 bins in \( Q^2 \), with similar statistics for the deuteron. The entire data set is available at the CLAS Physics Database or by request from the authors. These data can be used to constrain transition amplitudes for resonances of different spin and isospin which
FIG. 3: Results for the asymmetry $A_1(x)$ on the proton. Filled circles show our data in the deep inelastic region ($W > 2$ GeV, $Q^2 > 1$ GeV$^2$) while the remaining open symbols are for data from several previous experiments. The SU(6) expectation for all $x$ is indicated by the arrow. The solid line shows our parametrization of the world data at a fixed $Q^2 = 10$ GeV$^2$. The shaded band covers a range of calculations by Isgur et al. that model the hyperfine-interaction breaking of SU(6) symmetry. The remaining three curves correspond to different scenarios of SU(6) symmetry breaking as presented in the paper by Close and Mehndouch [17]: helicity-1/2 dominance (dashed), spin-1/2 dominance (dotted) and symmetric wave function suppression (dash-dotted).

partially overlap with each other and the non-resonant background. For instance, in the region of the $\Delta(1232)$, the asymmetry is negative at low $Q^2$, since the transition to the $\Delta$ is dominated by the $A_{3/2}$ amplitude, while at larger $Q^2$ this amplitude seems to be suppressed and the non-resonant background becomes more dominant. Similarly, around $W = 1.53$ GeV, the asymmetry makes a rapid transition from being slightly negative at small $Q^2$ to large positive values even at rather moderate $Q^2$, indicating that the $A_{3/2}$ amplitude for the transition to the $D_{13}$ resonance becomes less important than the $A_{1/2}$ amplitude for the transition to both the $D_{13}$ and $S_{11}$ resonances.

The closely related ratio of structure functions, $g_1/F_1$, is shown in Fig. 2 as a function of $Q^2$, averaged over several bins in $x$. The new data are in good agreement with the results of the first run with CLAS [12, 13]. In the DIS region, both $g_1$ and $F_1$ are expected to have only logarithmic scaling violations, and their ratio has been found to be nearly independent of $Q^2$ in previous experiments (see, for example, the SLAC data [3] reproduced in Fig. 2). Our data show a clear decrease in this asymmetry with decreasing $Q^2$; in particular, for the proton they fall below the DIS parametrization around $Q^2 = 1$ GeV$^2$ and small $x$. This $Q^2$-dependence becomes much more pronounced in the region of the nucleon resonances (at $Q^2$ below the limits indicated by arrows in Fig. 2), leading to a strong deviation of the data from a smooth extrapolation of DIS data [3] (dashed lines in Fig. 2). This is a direct consequence of the fact that $W$ varies with $Q^2$ at fixed $x$ and reflects the $W$-dependence seen in Fig. 1. For kinematics corresponding to the excitation of the $\Delta$ resonance (at the lowest $Q^2$ in each panel), the asymmetry is much reduced and even changes sign relative to the DIS region at small $Q^2$ due to the dominance of the $A_{3/2}$ amplitude. The data above $W = 2$ GeV can be incorporated into NLO fits of spin structure functions to improve the precision with which polarized parton distribution functions are known.

The results for $A_1(x)$, averaged over $Q^2 > 1$ GeV$^2$ and $W > 2$ GeV, are shown in Fig. 3 for the proton and in Fig. 4 for the deuteron. At small $x$, where our average $Q^2$ is close to 1 GeV$^2$, the data fall below our parametrization of the world data with $Q^2 = 10$ GeV$^2$ (solid line). This deviation is due to the $Q^2$-dependence shown in Fig. 4 (note that $A_1$ and $g_1/F_1$ are very close in this kinematic region). In contrast, both of our data sets exceed the SU(6) limits at $x$ above 0.45. The hyperfine interaction model of SU(6) symmetry breaking by
parametrization of the world data on $F_1^p$ and $F_1^d$:

$$\frac{\Delta u}{u} \approx \frac{5g_1^p - 2g_1^d/(1 - 1.5w_D)}{5F_1^p - 2F_1^d};$$

$$\frac{\Delta d}{d} \approx \frac{8g_1^d/(1 - 1.5w_D) - 5g_1^p}{8F_1^d - 5F_1^p}. \tag{3}$$

The result (Fig. 5) has relatively large statistical errors for $\Delta d/d$, since neither $A_2^p$ nor $A_2^d$ are very sensitive to $\Delta d/d$. (We included data down to $W = 1.77$ GeV in our estimate for the highest $x$ points to reduce those errors somewhat; at these rather large values of $Q^2 > 3$ GeV$^2$ we expect little deviation from the DIS limit in this $W$ range). Our estimate is consistent with the result from the $^3$He experiment [11], showing no indication of a sign change to positive values up to $x \approx 0.6$. At the same time, our data for $\Delta u/u$ are the statistically most precise available at this time, and show a consistent trend towards $\Delta u/u = 1$ at our highest $x$ points. While the absolute values of $\Delta u/u$ and $\Delta d/d$ might be somewhat different from more sophisticated NLO DGLAP analyses (like the curves shown in Fig. 5), the error bars in Fig. 5 give an indication of the possible improvement in precision when our data are included in such fits.

In summary, we have measured the virtual photon asymmetry $A_1$ and the related ratio $g_1/F_1$ of structure functions on the proton and the deuteron with unprecedented precision, at high $x$ and over a large kinematic range in $x$ and $Q^2$. Our data span the resonance region $W < 2$ GeV and extend into the DIS region. They contribute to our knowledge of the valence quark structure of the nucleon and its excited states, and can be used to improve NLO fits for the extraction of polarized parton distribution functions. Our data confirm a clear increase in the polarization of valence $u$ quarks at high $x$ as expected by pQCD and various models of SU(6) symmetry breaking; on the other hand, the polarization of the $d$ quarks seems to remain negative up to the highest values of $x$ accessible to our experiment. Future measurements, in particular with the energy-upgraded Jefferson Lab accelerator, will be able to extend these data with improved precision to higher values of $x$ (exceeding $x \approx 0.8$), allowing a definite test of various models of SU(6) symmetry breaking.

**Acknowledgments**

We would like to acknowledge the outstanding efforts of the staff of the Accelerator and the Physics Divisions at Jefferson Lab that made this experiment possible. This work was supported in part by the Italian Instituto Nazionale di Fisica Nucleare, the French Centre National de la Recherche Scientifique, the French Commissariat à l’Energie Atomique, the U.S. Department of Energy and National Science Foundation, the Emmy Noether

**FIG. 5:** Quark polarizations $\Delta u/u$ and $\Delta d/d$ extracted from our data. Included are all data above $W = 1.77$ GeV and $Q^2 = 1$ GeV$^2$. Also shown are semi-inclusive results from 

* Table 1* (grey band in figures) is closest to the data. Of the different mechanisms for SU(6) symmetry breaking considered by Close and Mehneckouk [17], the model with suppression of the symmetric quark wave function (dot-dashed curve in Figs. 3) deviates least from the data. In general, our results are in better agreement with models (like the two mentioned above) in which the ratio of down to up quarks, $d/u$, goes to zero and the polarization of down quarks, $\Delta d/d$, tends to stay negative for rather large values of $x$, in contrast to the behavior expected from hadron helicity conservation [13,16]. This is also in agreement with the findings by the experiment on $^3$He [11] in Jefferson Lab’s Hall A.

Within a naive quark-parton model (and ignoring any contribution from strange quarks), we can estimate the quark polarizations $\Delta u/u$ and $\Delta d/d$ directly from our data by combining the results for $g_1$ from the proton and the deuteron (including some nuclear corrections for the deuteron D-state and Fermi motion) with our

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*Note:** The text contains mathematical equations and figures that require careful reading and understanding of the context and symbols used. The paragraphs are structured to maintain coherence and flow, with key points highlighted for emphasis. The document is related to experimental results in nuclear physics, specifically focusing on quark polarization measurements at Jefferson Lab. The results are compared to theoretical models and previous experiments, highlighting the consistency and the improvement in precision achieved by the new data. The acknowledgments section credits the contributions of various institutions and individuals involved in the project.
grant from the Deutsche Forschung Gemeinschaft and the Korean Science and Engineering Foundation. The Southeastern Universities Research Association (SURA) operates the Thomas Jefferson National Accelerator Facility for the United States Department of Energy under contract DE-AC05-84ER-40150.

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